

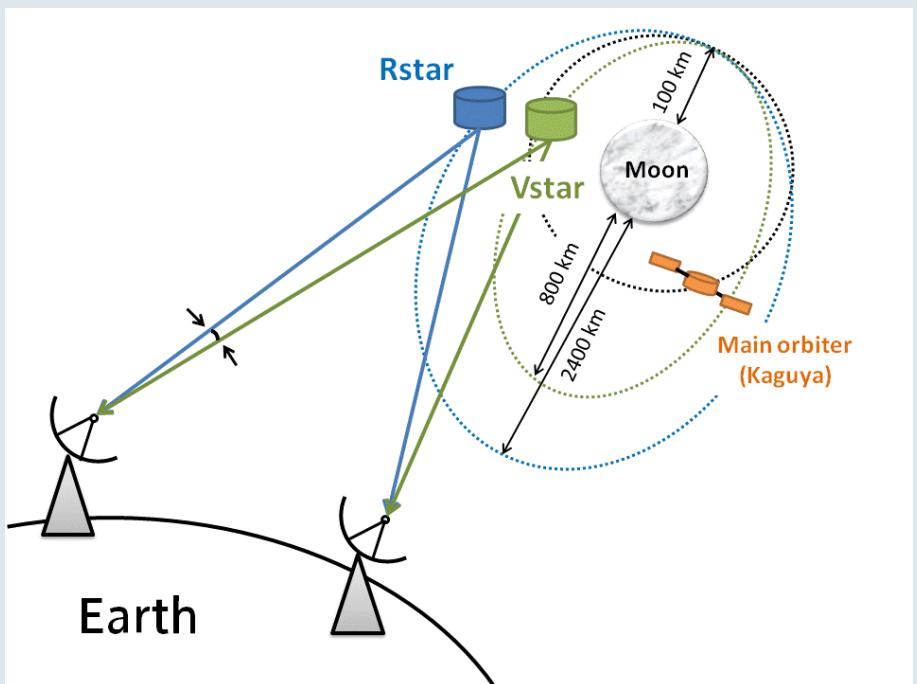
## Session 3

# Processing SELENE Differential VLBI Data

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- SELenological and ENgineering Explorer
  - JAXA, 2007-2009
  - 3 lunar satellites
- same-beam differential VLBI (D-VLBI)
  - improved orbit consistency from several hundreds to several tens of metres [Goossens et al., 2010]
- nominal accuracy  
 (differential phase delay rms):
  - 3.44 ps (1 mm) S-band  
 [Kikuchi et al., 2009]



- 2 datasets (from NAOJ Mizusawa):
  - October 2008, 17-22: 4 japanese antennas
  - January 2008, 12-16: 4 japanese antennas + intercontinental baselines



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- Implementation into VieVS
- Challenges:
  - *Moving sources at finite distance*
  - Relativistic time and coordinate transformations (TDB, TT, TCB, TCG resp. BDRS, TRS, BCRS, GCRS)
  - Consistent application of corresponding scaling factors (Lc, Lg, Lb)
- Good agreement of 3 models (< 1 ps resp. < 3 ps)
  - Sekido & Fukushima 2006
  - Fukushima 1994
  - Klioner 1991

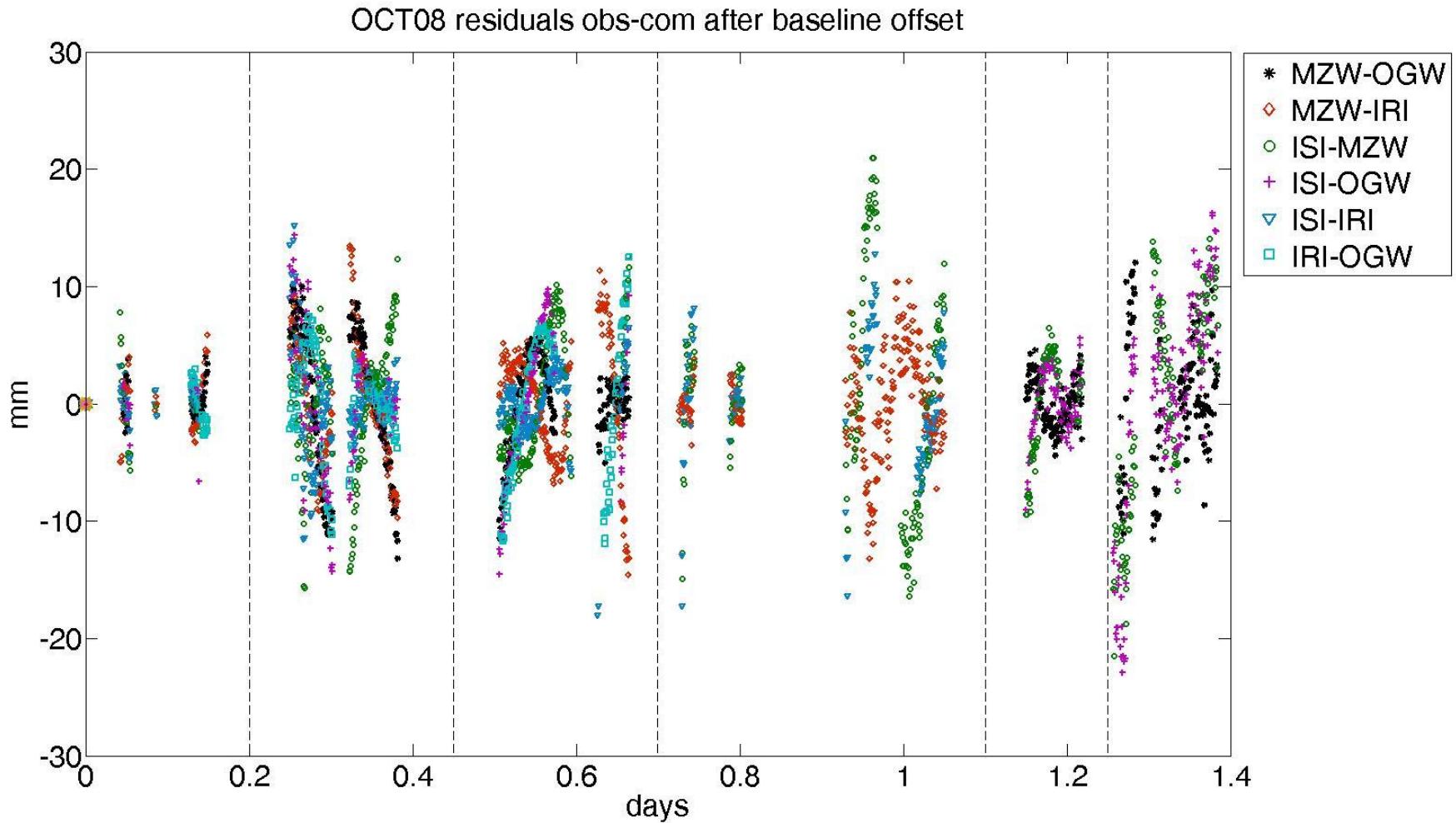


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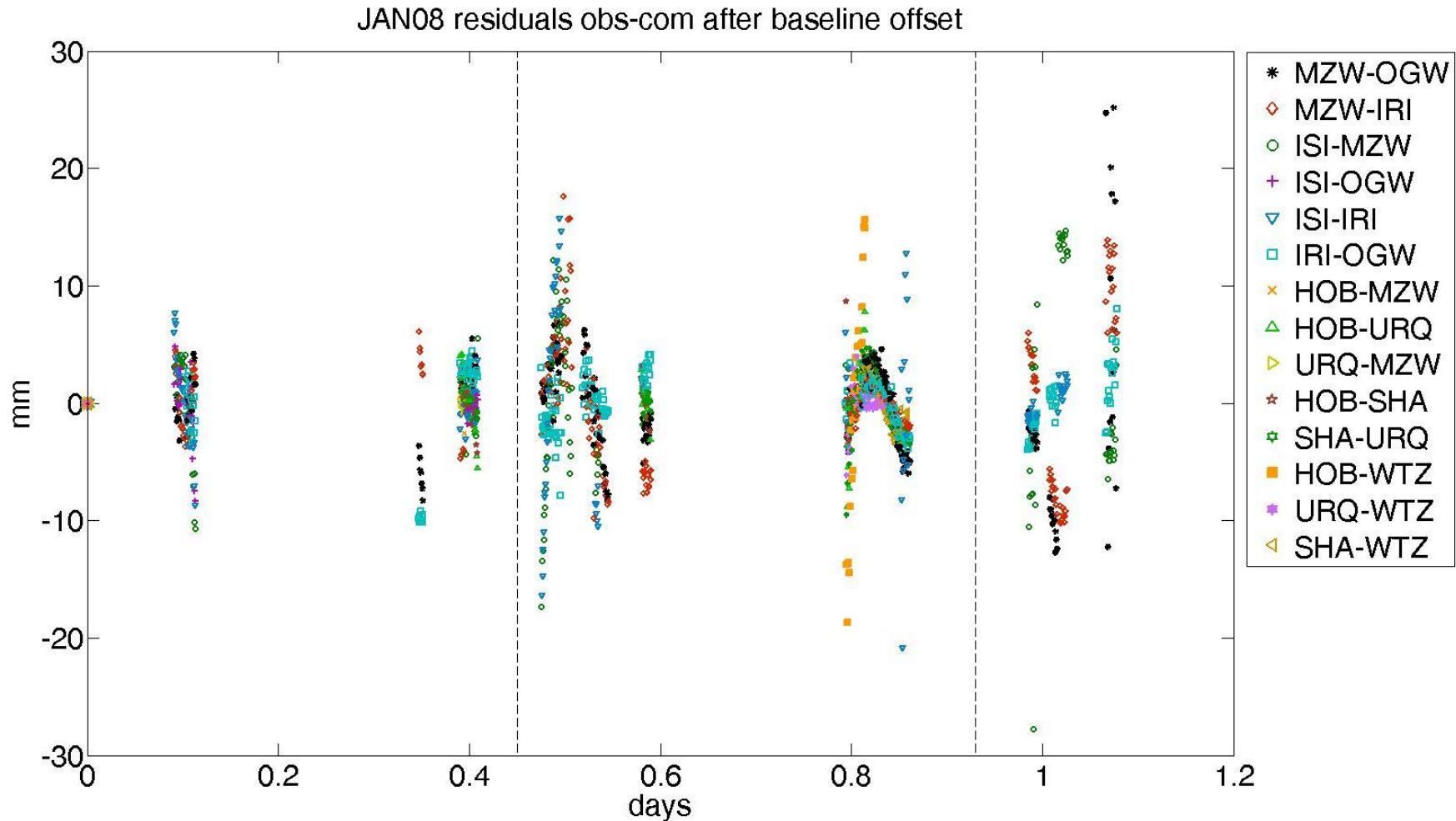


→ **Differences correspond to the theoretical values**

→ **Verification through comparison of 3 models**



$$\Delta\tau = \tau_{\text{RSTAR}} - \tau_{\text{VSTAR}}$$



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# Results / Comparison



- Residuals are at the same level as those from NAOJ  
 $\pm 10 \text{ mm (30 ps)}$
- NAOJ explains residuals with  
*„probably mismodelling of solar radiation pressure“*

(long baselines)	$\tau$	$\Delta\tau$
<b>GEOMETRY:</b>		
Antenna $\pm$ 5cm	300 ps	1-2 ps
Orbit $\pm$ 10 m	150 -1000 ps	2-8 ps
EOP	5 ps (60 ps)	< 0.05 (0.1) ps
dUT1: 5 ms		
xp, yp: 200 mas		
dX, dY: 300 mas		

## (long baselines)

$\tau$

$\Delta\tau$

### GEOMETRY:

Antenna  $\pm 5\text{cm}$

300 ps

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Orbit  $\pm 10\text{ m}$

150 -1000 ps

2-8 ps

EOP

5 ps (60 ps)

< 0.05 (0.1) ps

dUT1: 5 ms

usual elev > 20°  
min. elev. 10° (5°)

xp, yp: 200 mas

dX, dY: 300 mas

### ATMOSPHERE:

Trop\_hydr

2-20 (10-60) ns

30-300 (50-1000) ps

a priori

Trop\_wet

1-3 (4) ns

4-40 (10-60) ps

ECMWF

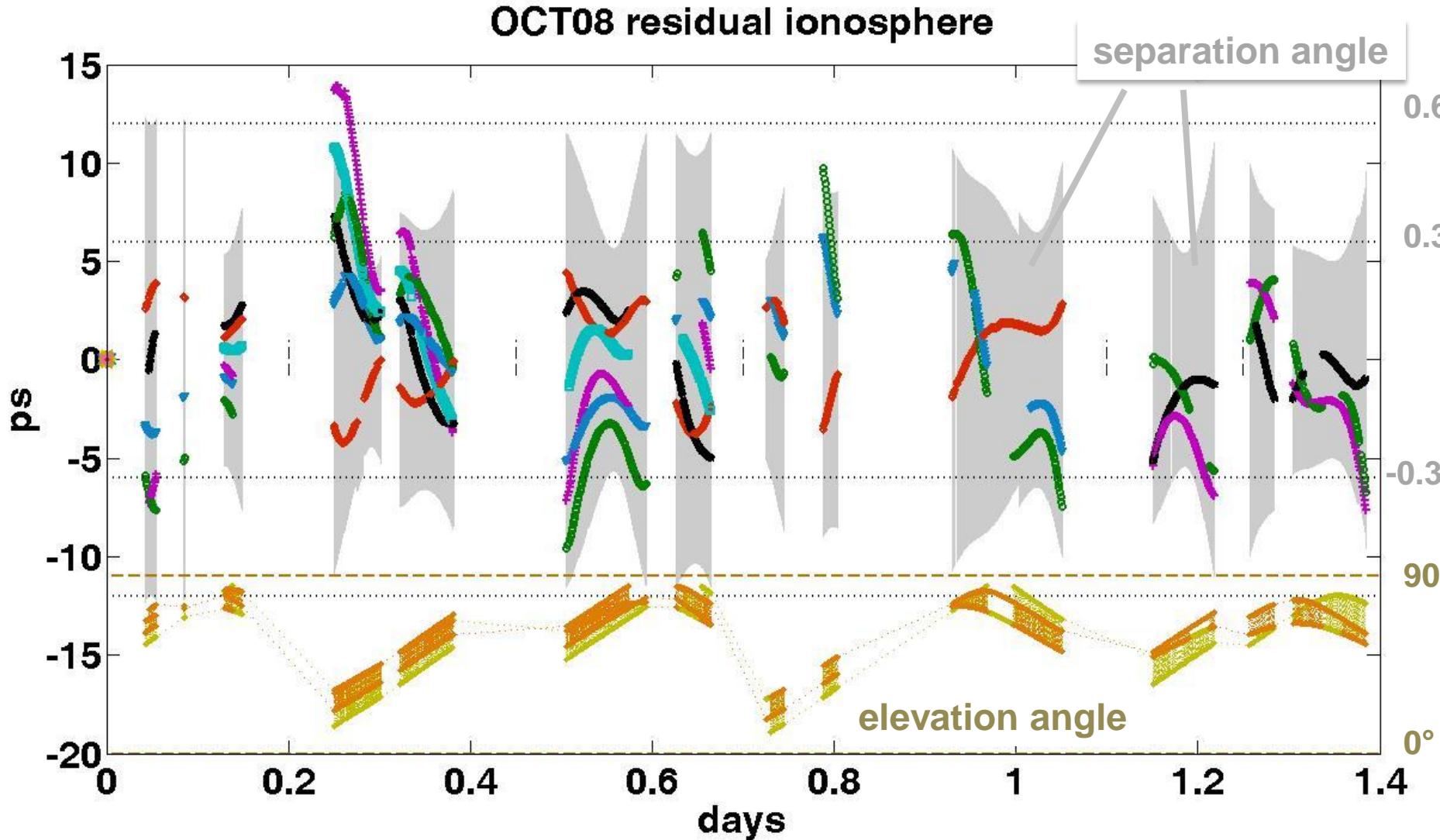
Ionosphere

1.5 (2-10) ns

10 (80) ps

TEC-maps

Peak at noon; nearly all observations during the night



# simulated turbulence

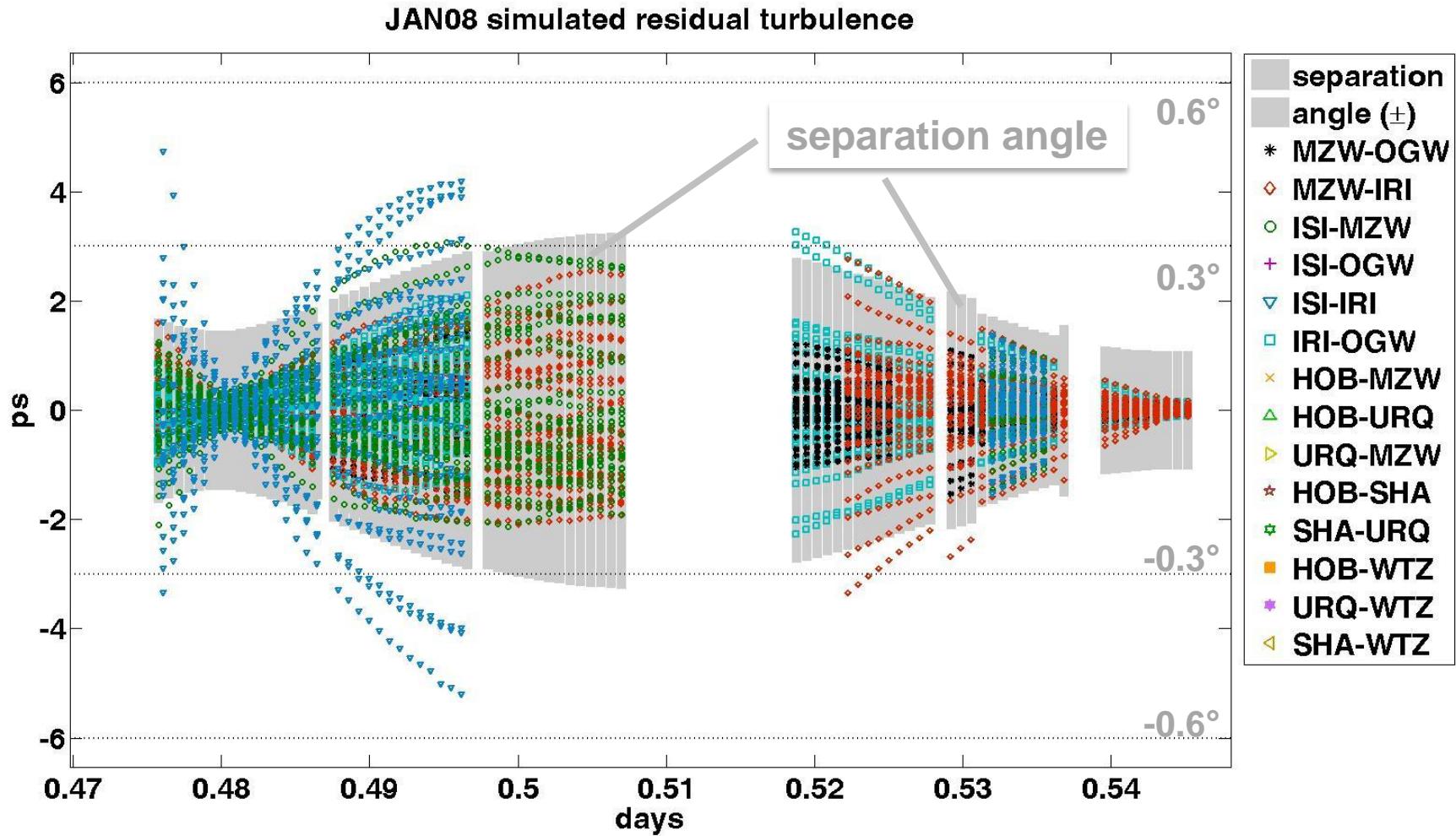


→ VieVS-simulator [Pany et al., 2010]; N = 30

# simulated turbulence



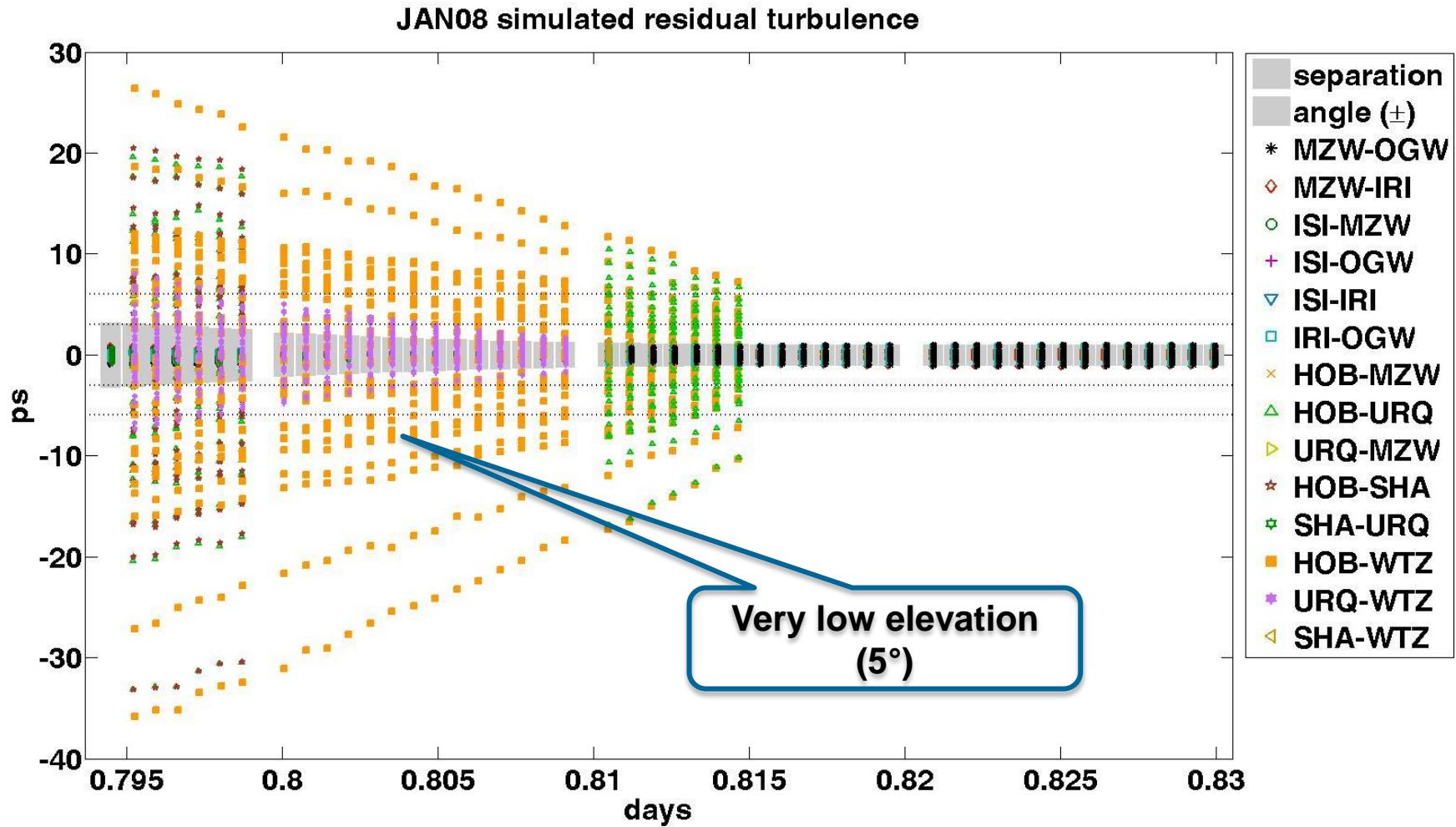
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# simulated turbulence



→ VieVS-simulator [Pany et al., 2010]; N = 30



# Results / Comparison (2)



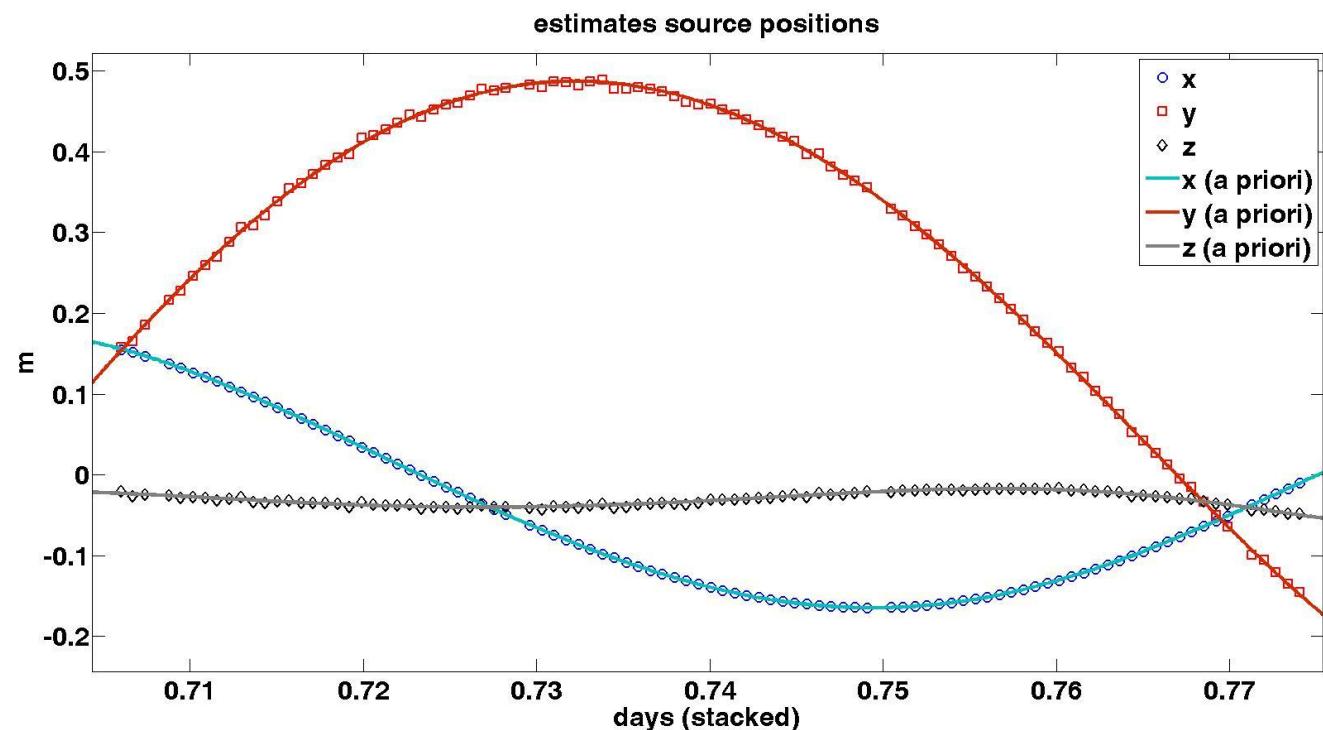
- Geometric effects (station coordinates, source coordinates, EOP) are nearly cancelled out.
- Residual tropospheric effects can reach the level of significance.
  - *Particularly for intercontinental baselines.*
- But: Applying wet troposphere and ionospheric corrections doesn't improve the result significantly.
  - *Some residuals decrease but some others increase.*

$$\begin{aligned}
 \Delta\tau &= \tau_{RSTAR} - \tau_{VSTAR} = \\
 &= [(RSTAR - St1) - (RSTAR - St2)] - [(VSTAR - St1) - (VSTAR - St2)]
 \end{aligned}$$

$$\frac{\partial\Delta\tau}{\partial VSTAR} = -\frac{VSTAR - St1}{r_{VSTAR-St1}} + \frac{VSTAR - St2}{r_{VSTAR-St2}}$$

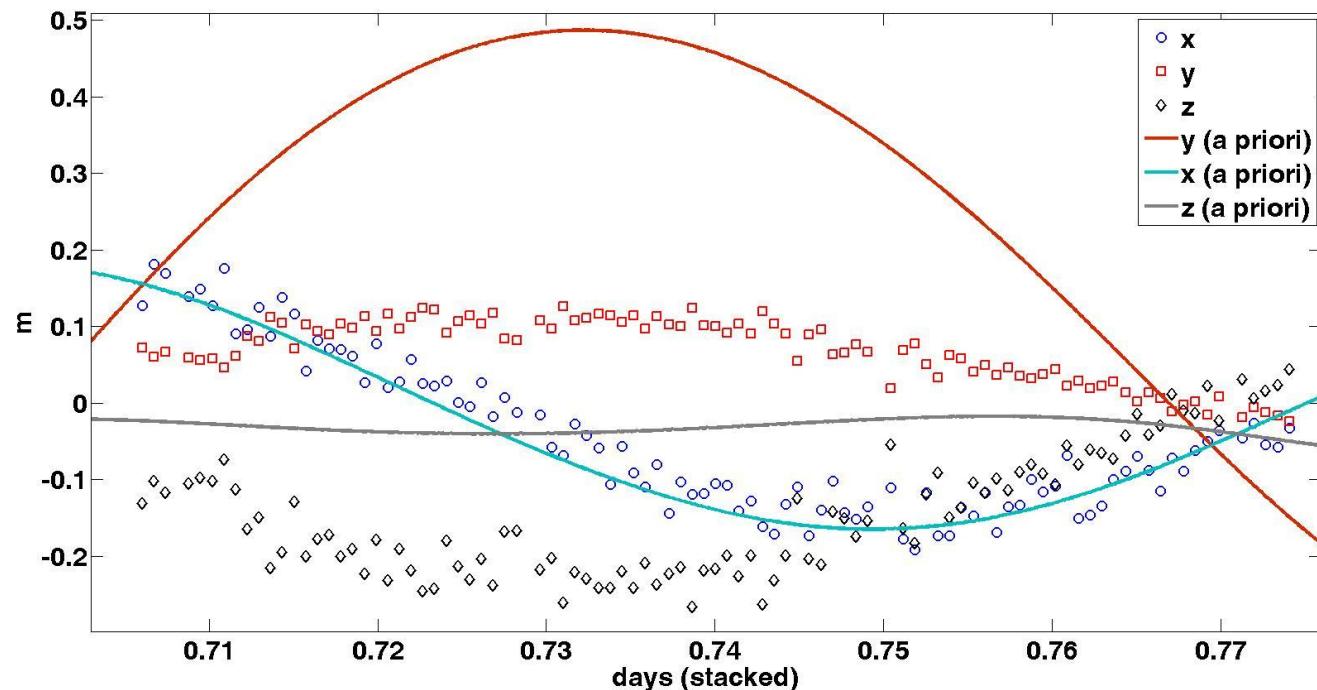
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 \end{aligned}$$

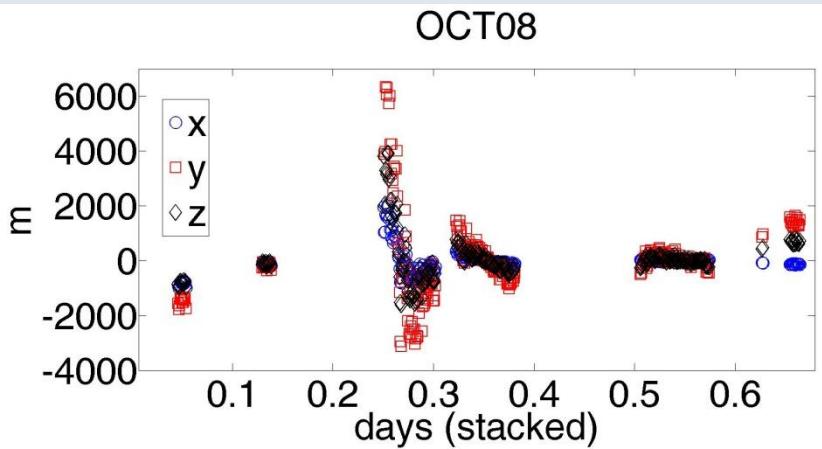
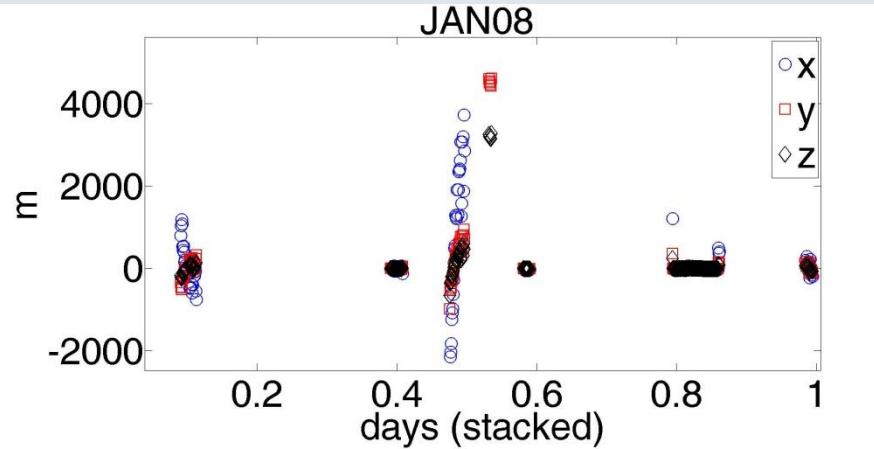
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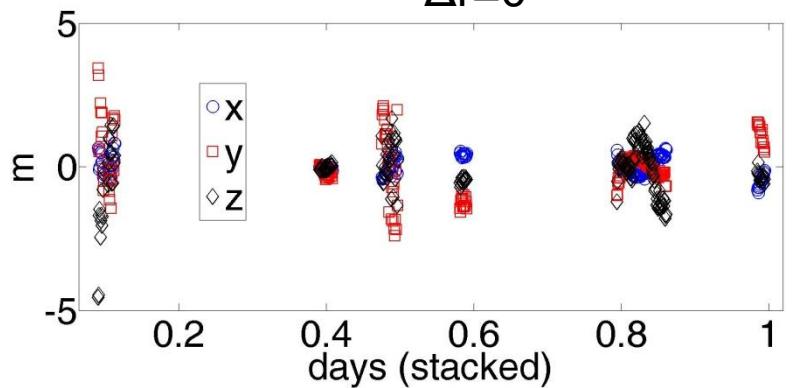
 **1 ps noise:** OCT08:  $\pm 100$  m  
**JAN08:**  $\pm 50$  m

 **implement condition  $\Delta r = 0$**

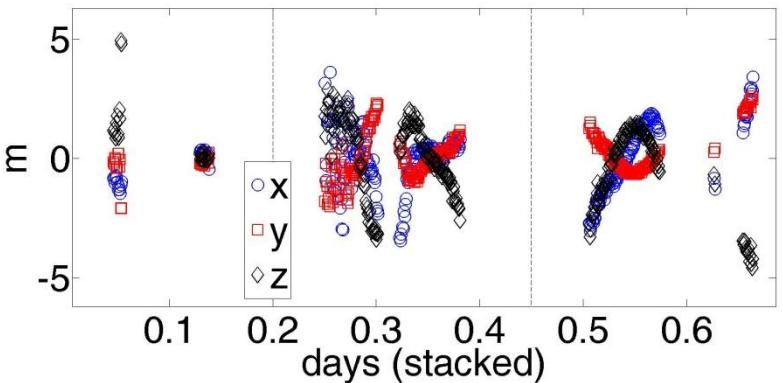




JAN08    $\Delta r=0$



OCT08    $\Delta r=0$



# Results / Comparison (3)

- Model for orbit estimation (xyz) is correct, but highly correlated and unstable.
- *Possible solution:*  $\Delta r = 0$
- NAOJ: *total orbit errors at an average level of 18m*
- Estimates: several km → some m
- Goal: find better strategies
  - *Line of sight*
  - *estimate orbit parameters*
- **Upcoming: Studying estimation strategy with VLBI observations to GNSS-satellites.**

# THE END

*Thank You for listening!*

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## References:

- Goossens et al., 2010: *Lunar gravity field determination using SELENE same-beam differential VLBI tracking data*, J. of Geodesy, DOI: 10.1007/s00190-010-0430-2.
- Kikuchi et al., 2009: *Pico-second accuracy VLBI of the two sub-satellites of SELENE (KAGUYA) using multi-frequency and same-beam methods*, Radio Sci. 44(RS2008).
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- Sekido & Fukushima, 2006: *A VLBI delay model for radio sources at a finite distance*, J. of Geodesy, 80:137-149, DOI 10.1007/s00190-006-0035-y.
- Pany et al., 2010: *Monte Carlo simulations of the impact of troposphere, clocks and measurement errors on the repeatability of VLBI positions*. J. of Geodesy, DOI: 10.1007/s00190-010-0415-1.