

# Observing GNSS L-band signals: ionospheric corrections by co-located GNSS measurements

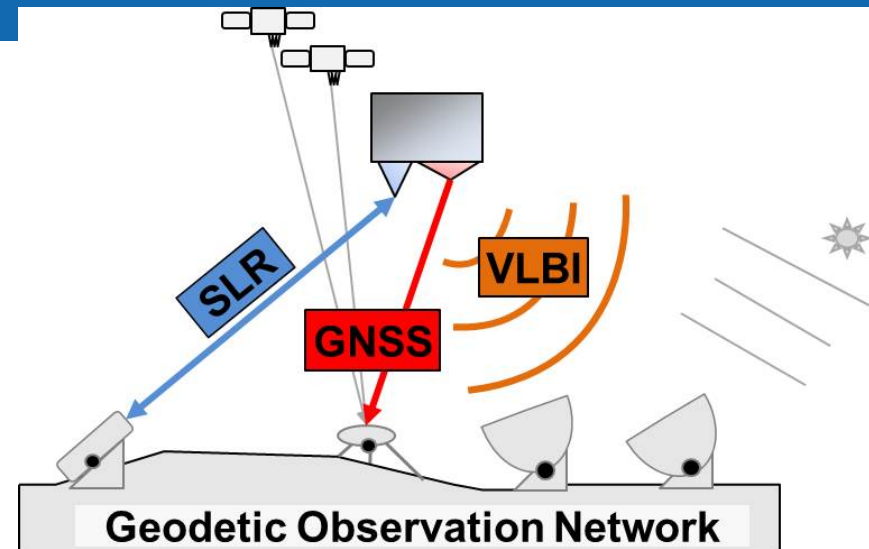
B. Männel and M. Rothacher

based on:

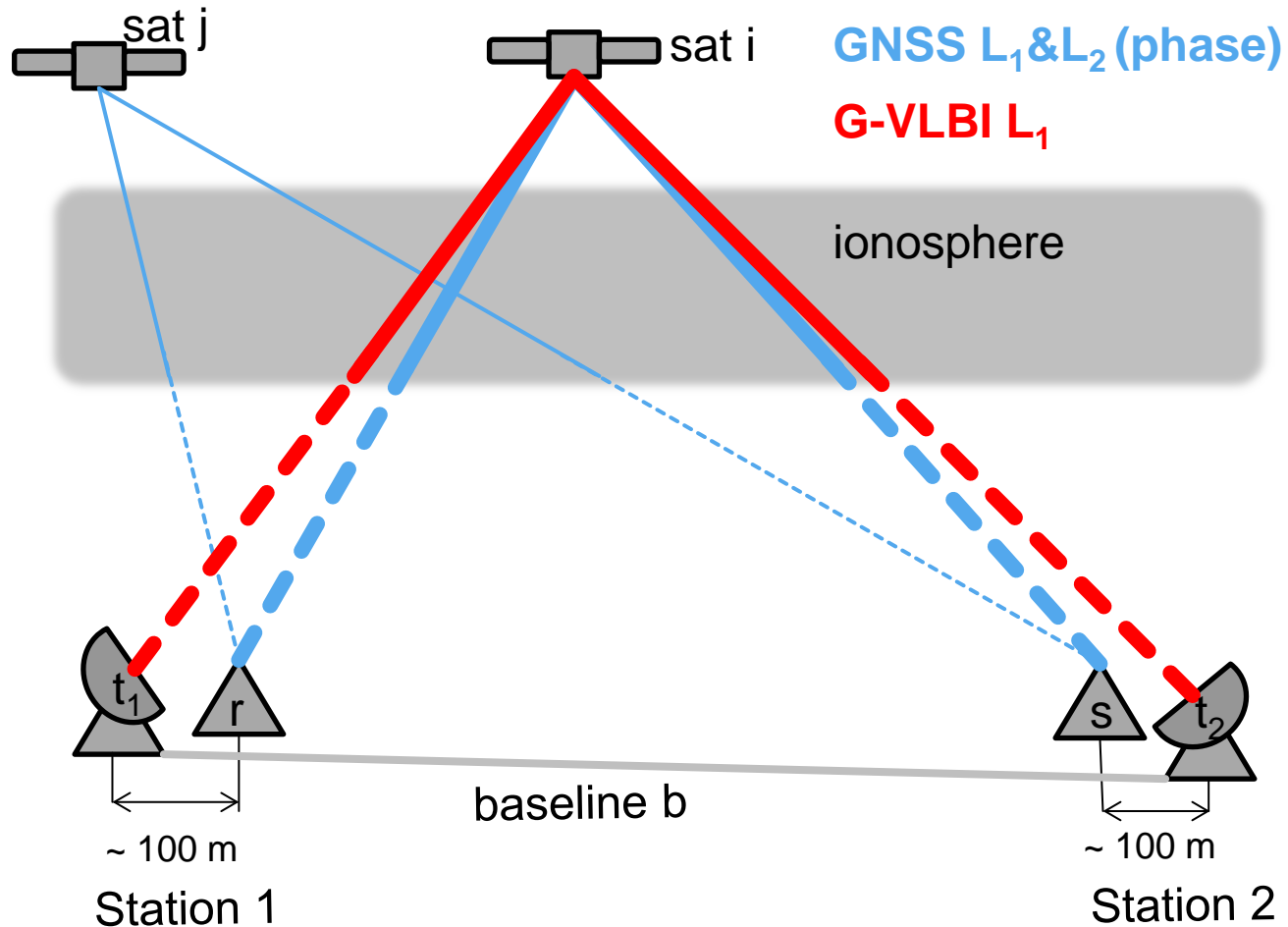
Männel, B. and Rothacher, M.: Ionospheric corrections for single-frequency VLBI observations by co-located GNSS measurements, submitted to Journal of Geodesy

# Motivation

- **G-VLBI**: independent observation of GNSS satellites using radio telescopes
- Advantages of G-VLBI observations:
  - Co-location in space for **GNSS, SLR and VLBI**
  - Improved investigations on ties and technique-specific error sources
  - Common parameters (e.g. atmospheric delays, orbits)
- G-VLBI might be limited to single-frequency → **ionospheric corrections**
  - GNSS-based model or GNSS-based local VTEC estimations
  - **Usage of the GNSS signal measured by a co-located GNSS antenna?**



# The L4R approach – Idea



# The L4R approach – Implementation

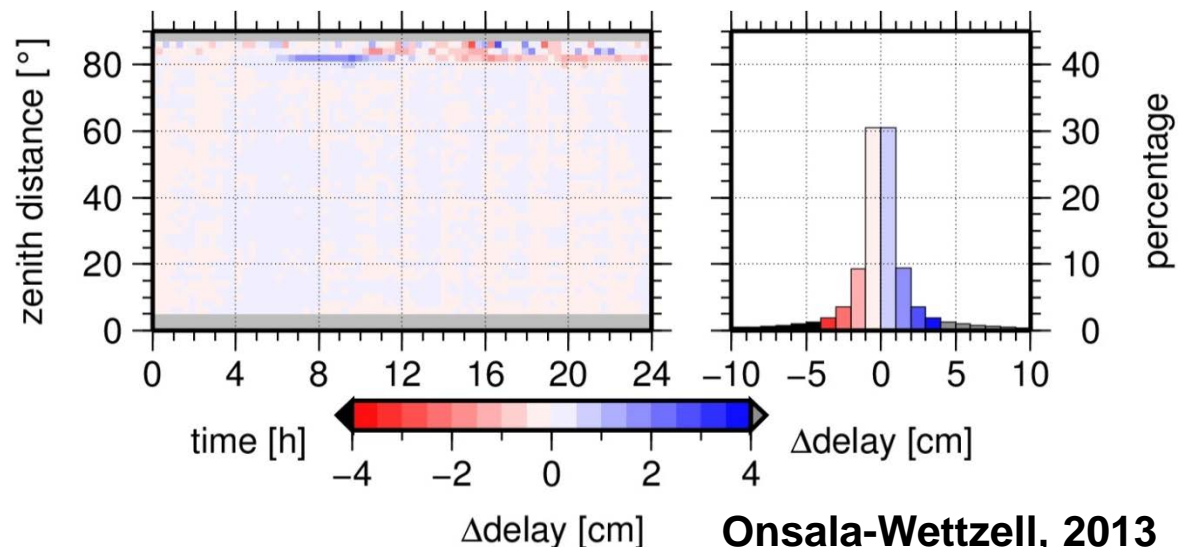
geometry-free  $L_4$  double  
difference residuals  
(ambiguities resolved)



split residuals to single  
differences

$$L_{rs,4}^{ij} = L_{rs,1}^{ij} - L_{rs,2}^{ij} = \lambda_1 N_1 - \lambda_2 N_2 + \frac{f_2^2 - f_1^2}{f_1^2 f_2^2} I_{rs}^{ij}$$

zero-mean condition per epoch: split  $n$  double diff. residuals into  $n+1$  single diff. residuals



Onsala-Wettzell, 2013

# The L4R approach – Implementation

geometry-free  $L_4$  double  
difference residuals  
(ambiguities resolved)



split residuals to single  
differences



(optional) split residuals to  
zero differences



add absolute ionospheric  
value from model



ionospheric correction

$$L_{rs,4}^{ij} = L_{rs,1}^{ij} - L_{rs,2}^{ij} = \lambda_1 N_1 - \lambda_2 N_2 + \frac{f_2^2 - f_1^2}{f_1^2 f_2^2} I_{rs}^{ij}$$

zero-mean condition per epoch: split  $n$  double diff. residuals into  $n+1$  single diff. residuals

zero-mean condition per epoch: split  $n$  single diff. residuals into  $n+1$  zero diff. residuals

$$I_{rs}^i = \text{absolute} + \text{relative} = \bar{I}_{rs} + \hat{I}_{rs}^i$$

Absolute part  $\bar{I}_{rs}$  is derived from CODE Global Ionosphere Models (GIMs)

# The L4R approach – Error sources

Effect	Impact on ionospheric delay corrections	Possibilities for improvements
GNSS multipath effects	<ul style="list-style-type: none"><li>• negligible for typical VLBI baselines (<math>&gt; 100</math> km)</li></ul>	---
Unresolved phase ambiguities	<ul style="list-style-type: none"><li>• Estimated ambiguities partially absorb ionospheric delays</li><li>• residuals 50cm smaller than in reality for a 5000 km baseline</li></ul>	<ul style="list-style-type: none"><li>• improved ambiguity resolution strategy (esp. for GLONASS)</li></ul>
Quality of CODE GIM's	<ul style="list-style-type: none"><li>• Smoothing effect has a direct impact on ionospheric delay correction</li></ul>	<ul style="list-style-type: none"><li>• usage of models with a higher resolution (temporal, spatial)</li></ul>

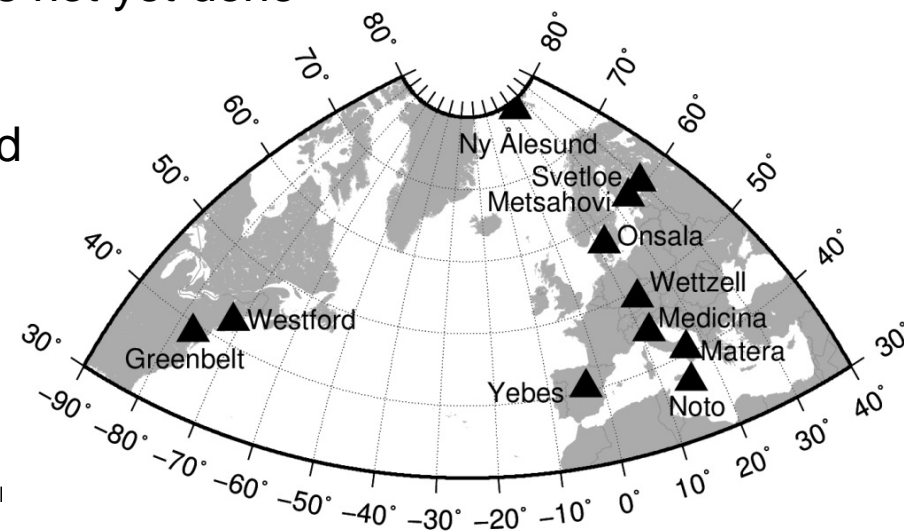
# The L4R approach – Validation

- Currently implemented in Bernese GNSS Software 5.2 (project version)
  - Estimation of corrections on single and zero difference level
  - Introduction of corrections to further processing steps

- Validation steps:

- Tests using real G-VLBI observations not yet done
  - V1: impact on GNSS  $L_1$  processing
  - V2: comparison against VLBI-derived ionospheric delays

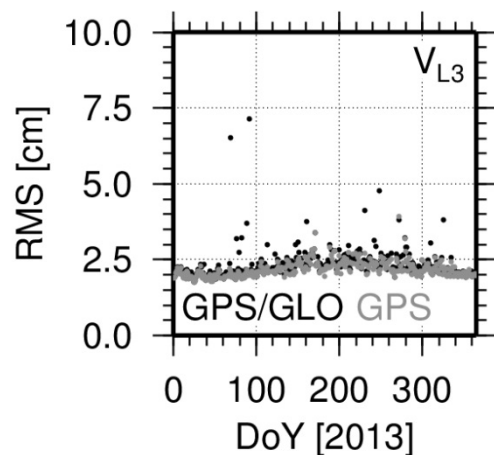
- GNSS and VLBI data from 2013 used



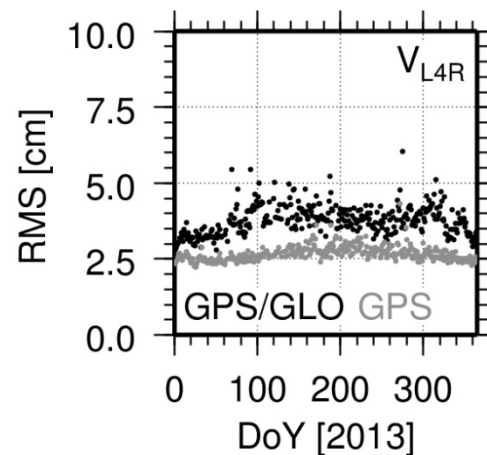
# Validation 1: GNSS $L_1$ processing

- Matera – Wettzell (~1000 km): Baseline MTWR and 0A0M (co-located baseline)
- RMS of residuals

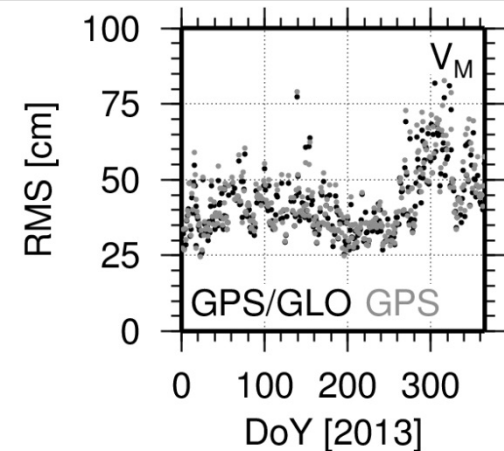
$L_3$  (two freq.)



$L_1$  + L4R (same basel.)



$L_1$  + CODE GIM's

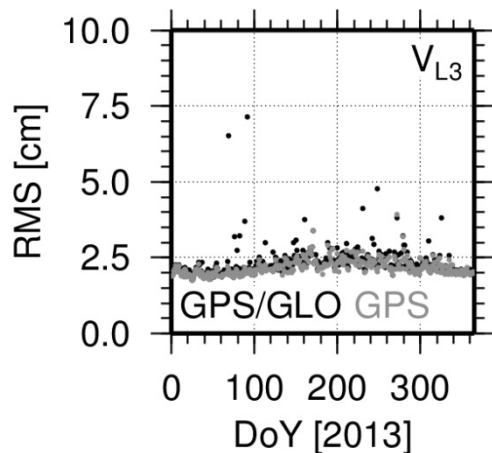




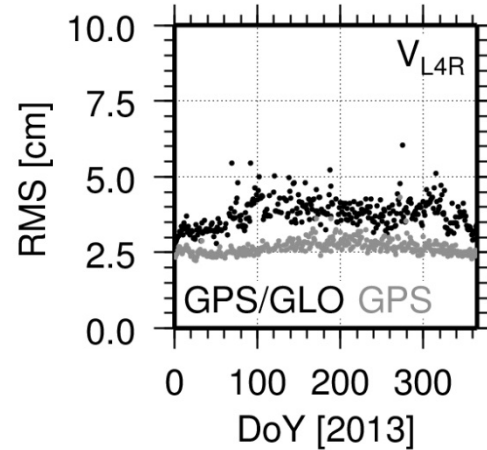
# Validation 1: GPS/GLO and 0A0M (co-located baseline)

- Matera – Wettzell (~1000 km)
- RMS of residuals

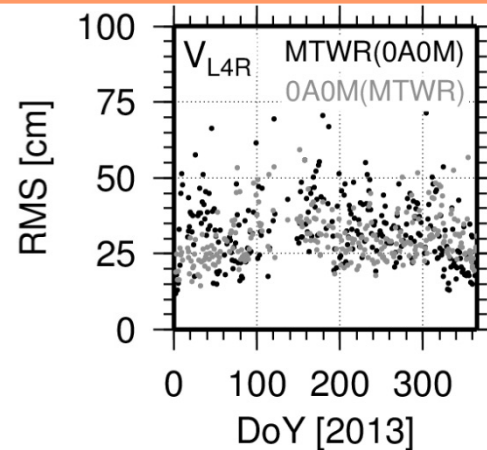
$L_3$  (two freq.)



$L_1 + L4R$  (same basel.)

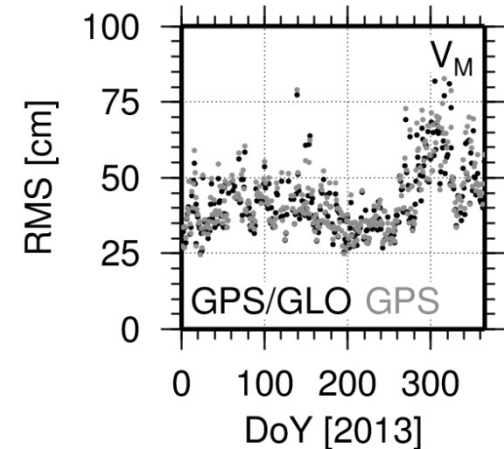


$L_1 + L4R$  (co-loc. basel.)



and 0A0M (co-located baseline)

$L_1 + \text{CODE GIM's}$

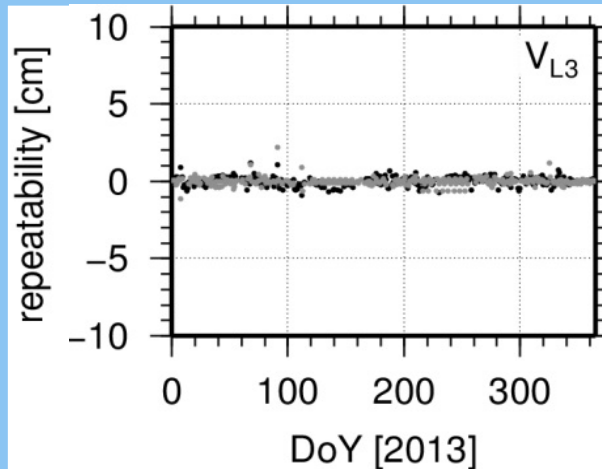


# Validation 1: GNSS $L_1$ processing

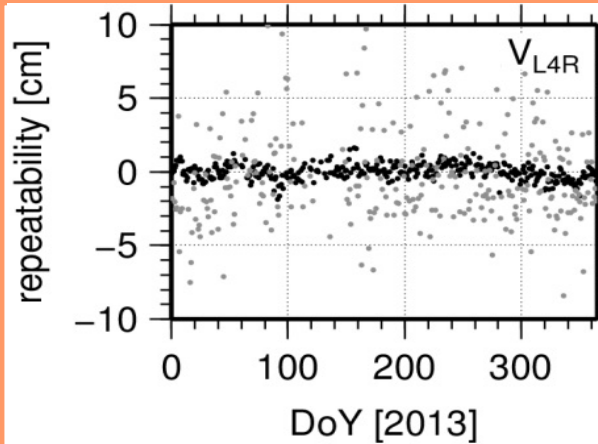
- RMS of station height repeatability

MTWR  
0A0M (MTWR)

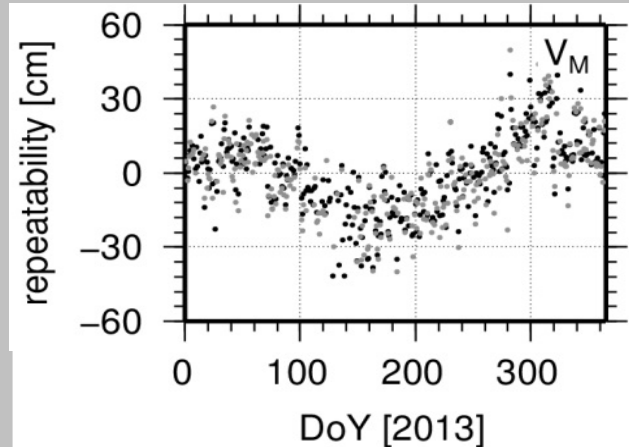
$L_3$  (two freq.)



$L_1$  + L4R from MTWR



$L_1$  + CODE GIM's



## Validation 2: VLBI-derived ionosphere delay

- GNSS and quasar observation same epoch, same direction ( $2^\circ$ ,  $\Delta t=15\text{min}$ )
- Difference L4R – VLBI ionospheric delay

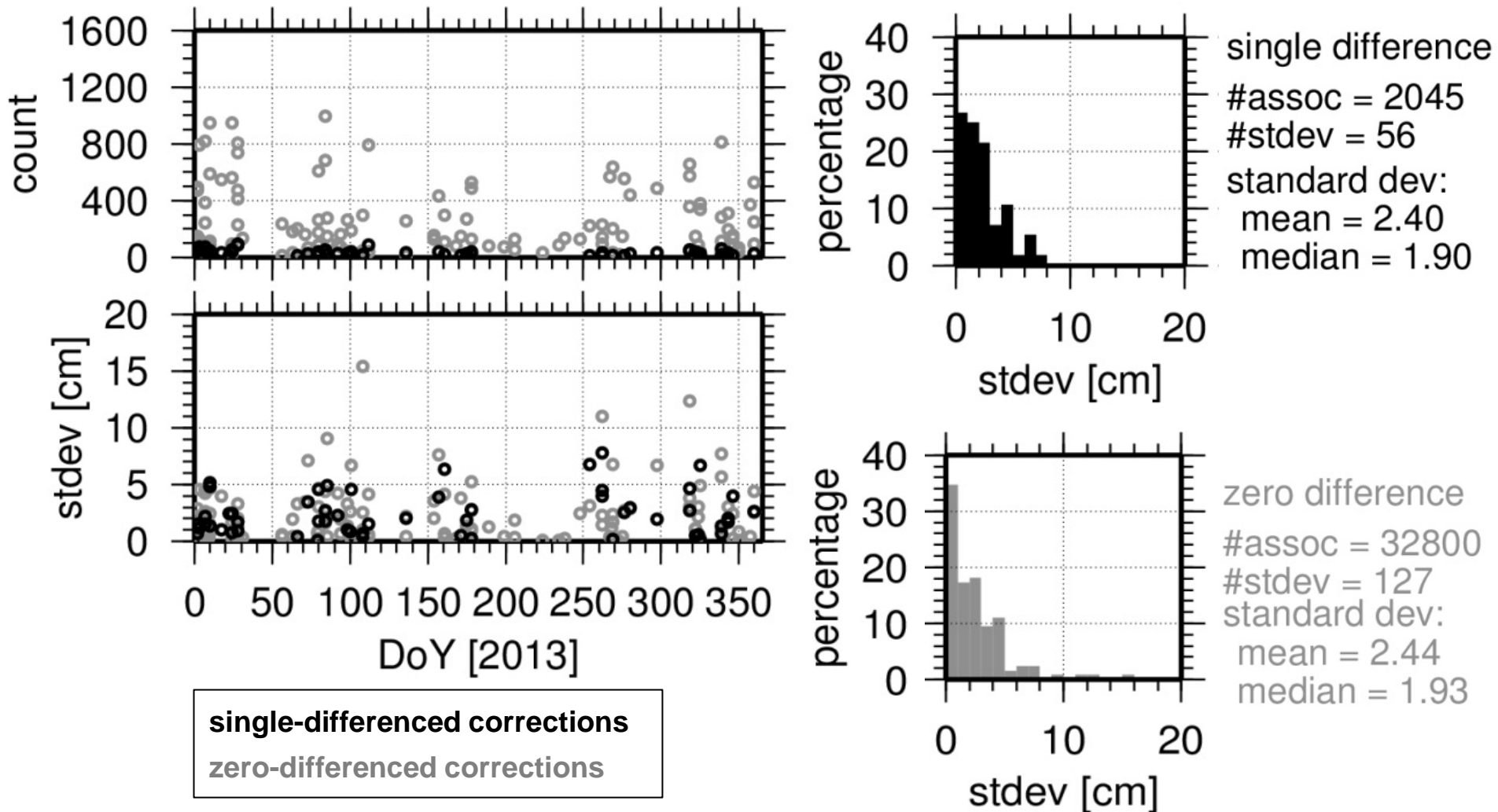
- Ionospheric delay correction: 
$$\tau'_{ion}(t) = \frac{f_S^2}{f_X^2 - f_S^2} (\tau_X - \tau_S) + \Delta\tau_{inst}$$

- $\Delta\tau_{inst}$  assumed to be constant over one session

Analysis of differences after  
subtracting session-wise mean  
values

Analysis of session-wise standard  
deviations

## Validation 2: VLBI-derived ionosphere delay



# Applications for L4R and conclusions

- GNSS-derived delay corrections are accurate to 2-5 cm
- G-VLBI
  - Usage of same signals to derive ionospheric corrections
  - Only very long baselines problematic (insufficient ambiguity resolution)
  - **High potential for G-VLBI applications**
- Quasar observations
  - GNSS satellite constellation vs. quasar observation schedule
  - Baseline length very critical (single diff. case)
  - **Only possible to a very limited extent**
- **Tests using real G-VLBI have to be done**

# Thank You

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