SPACE OBSER



CONT14 as a testbed for the combination of VLBI and GPS data on the observation level

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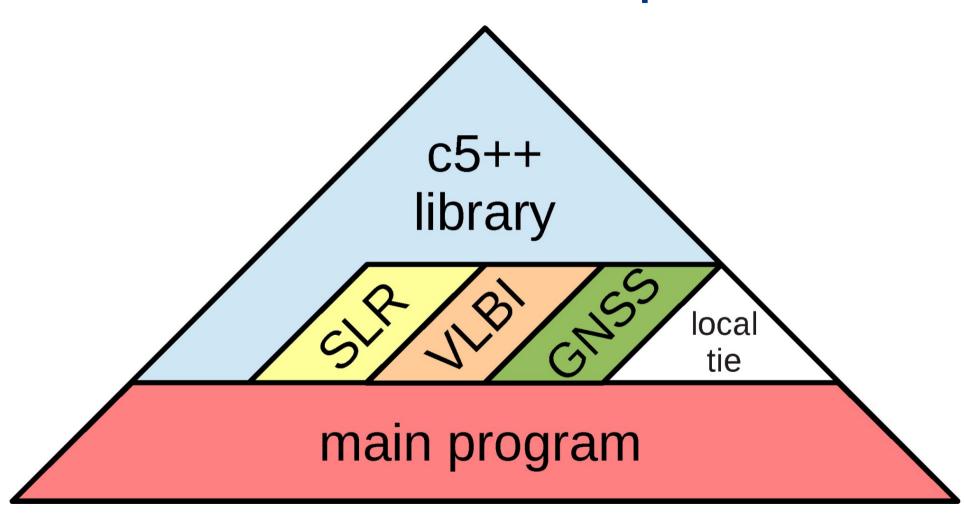






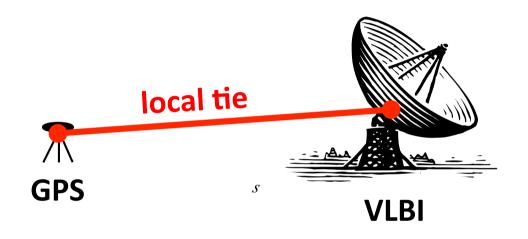


c5++ concept





Local ties



$$\sqrt{(\Delta x)^{2} + (\Delta y)^{2} + (\Delta z)^{2}} - \sqrt{(x_{V} - x_{G})^{2} + (y_{V} - y_{G})^{2} + (z_{V} - z_{G})^{2}} = 0 \pm \sigma$$
"O - C"



Local ties

NOTE 1: We don't introduce ties as 3D vectors, but only use the (invariant!) distance between the instruments as constraint

$$\sqrt{(\Delta x)^{2} + (\Delta y)^{2} + (\Delta z)^{2}} - \sqrt{(x_{V} - x_{G})^{2} + (y_{V} - y_{G})^{2} + (z_{V} - z_{G})^{2}} = 0 \pm \sigma$$
"O - C"



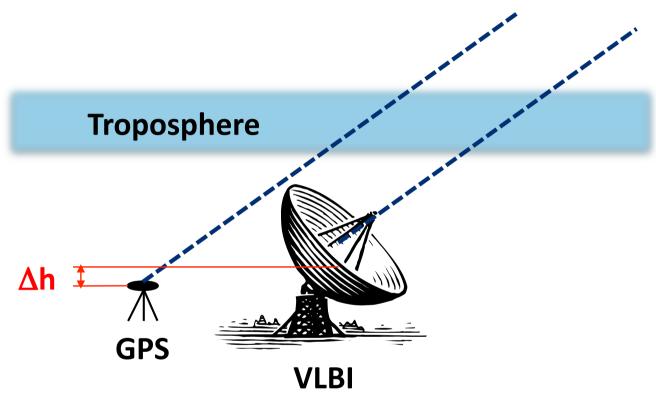
Local ties

NOTE 2: We don't use the formal errors from the site survey, but weight the constraints based on VCE results

$$\sqrt{(\Delta x)^{2} + (\Delta y)^{2} + (\Delta z)^{2}} - \sqrt{(x_{V} - x_{G})^{2} + (y_{V} - y_{G})^{2} + (z_{V} - z_{G})^{2}} = 0 \pm \sigma$$
"O - C"



"Troposphere ties"



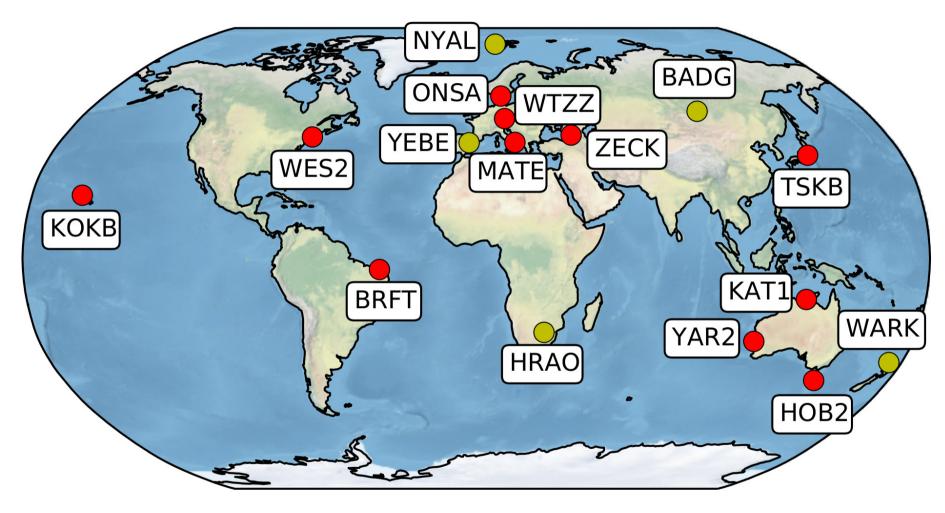
 $\tau_{GPS} = ZHD \cdot mf_h(\varepsilon) + ZWD \cdot mf_w(\varepsilon) + mf_g(\varepsilon) \cdot (G_N \cos \alpha + G_E \sin \alpha)$ $\tau_{VLBI} = \tau_{GPS} + \Delta D \cdot mf_h(\varepsilon)$



Variance component estimation (VCE)

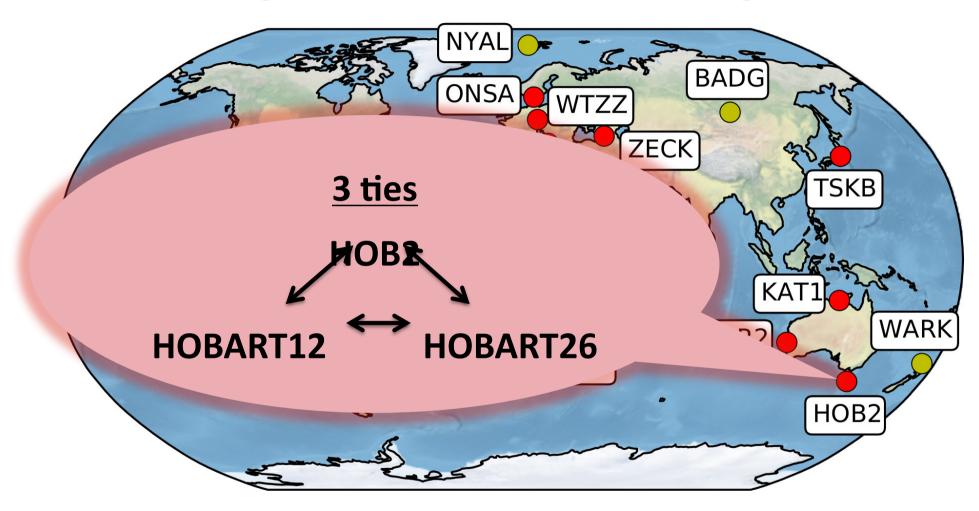
- Implemented via simplified Helmert method
- Allows to estimate one VC for
 - VLBI
 - SLR (not used in this presentation)
 - (all) local ties [note: highly unbalanced VCE]
 - GPS code phase measurements / site
 - GPS carrier phase measurements / site





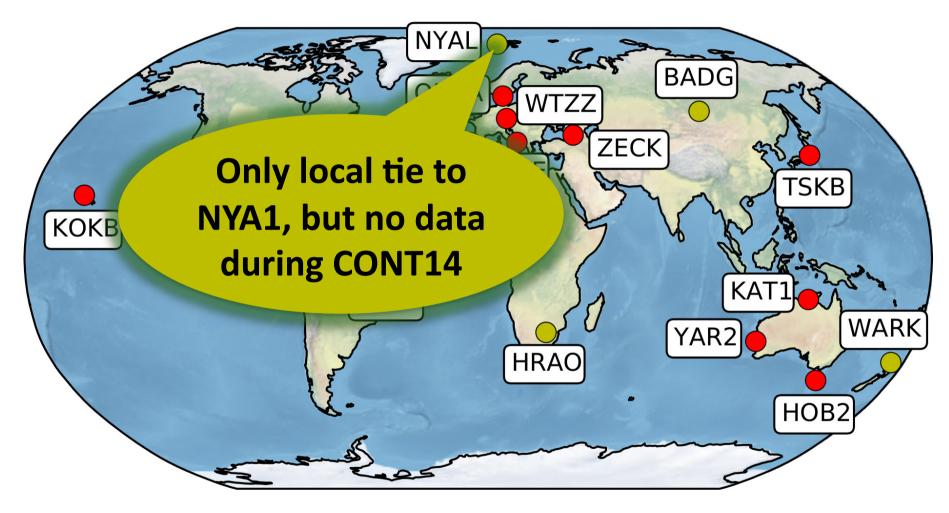
Local tie available in SINEX





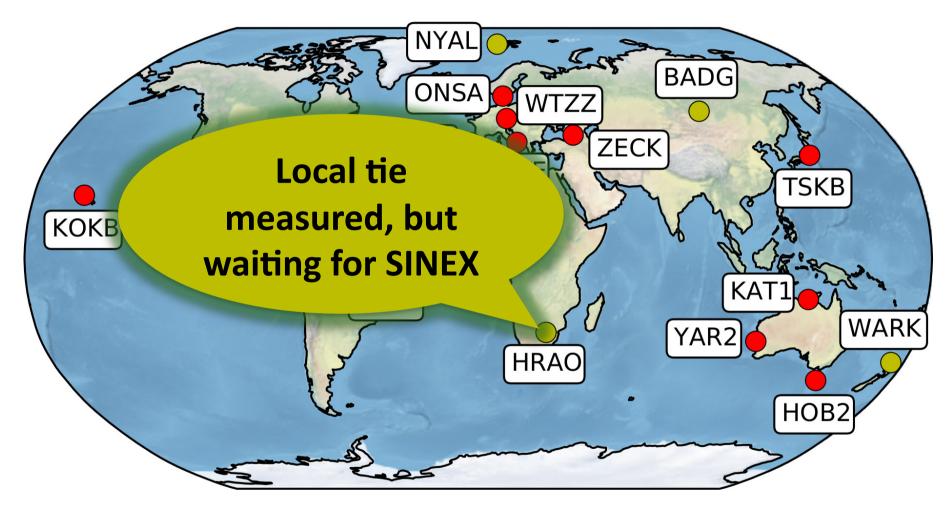
Local tie available in SINEX





Local tie available in SINEX

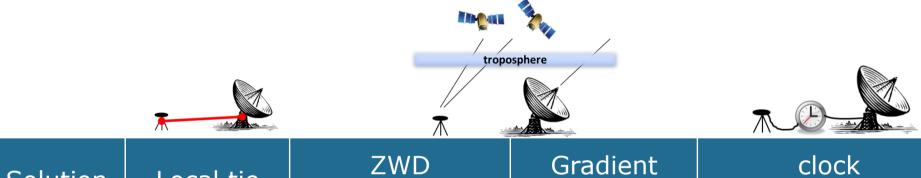




Local tie available in SINEX



Parameterization for the 15 daily solutions

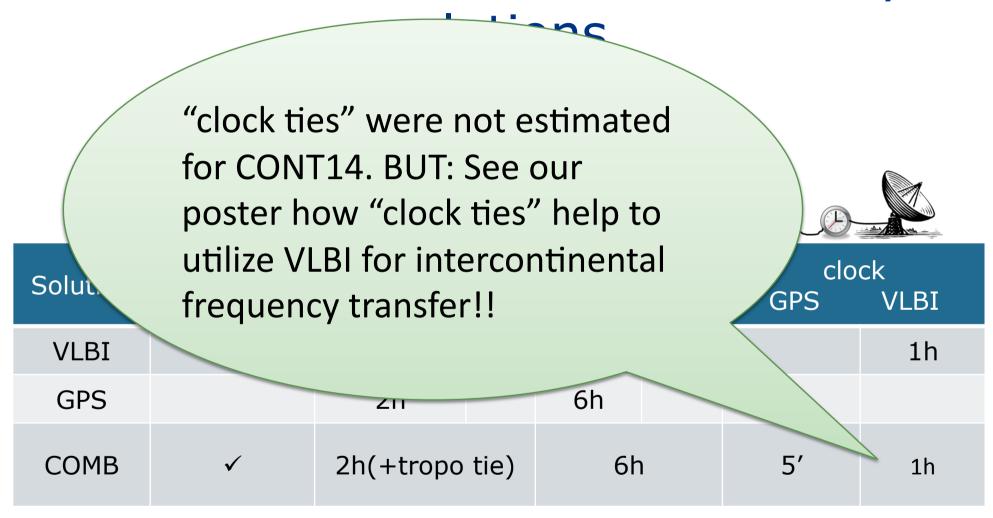


Solution	Local tie	ZWD GPS VLBI		Gradient GPS VLBI		clock GPS VLBI	
VLBI			2h		6h		1h
GPS		2h		6h		5′	
СОМВ	✓	2h(+tropo	tie)	6h	l	5′	1h

(All parameters estimated as piece-wise linear offsets)



Parameterization for the 15 daily



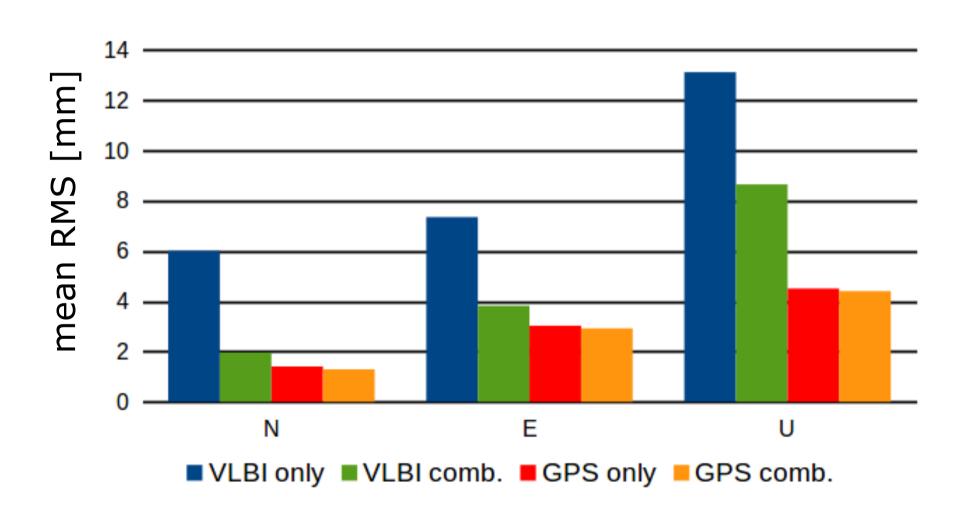
(All parameters estimated as piece-wise linear offsets)



Results



Station position repeatability





$\boldsymbol{\varTheta}$	Code	Carrier	
[mm]	phase	phase	
BADG	526.4 ± 9.5	3.4 ± 0.1	
FORT	294.1 ± 10.8	4.7 ± 1.1	
HRAO	666.6 ± 12.0	2.5 ± 0.3	
HOB2	317.8 ± 16.9	3.5 ± 0.5	
KAT1	323.2 ± 8.1	3.0 ± 0.2	
KOKB	709.8 ± 17.9	3.3 ±0.2	
MATE	376.3 ± 20.2	2.8 ± 0.3	
NYAL	414.3 ± 10.6	2.1 ± 0.2	

<i>⊖</i> [mm]	Code phase	Carrier phase
ONSA	425.1 ± 7.3	2.6 ± 0.1
TSKB	557.6 ± 22.5	3.1 ± 0.4
WARK	839.2 ± 11.5	4.2 ± 0.4
WES2	405.1 ± 13.4	3.3 ± 0.3
WTZZ	628.1 ± 12.3	4.3 ± 0.3
YAR2	849.3 ± 14.3	2.5 ± 0.5
ZECK	509.5 ± 9.3	3.7 ± 0.3

GPS



	Θ	Code	Carrier	$\boldsymbol{\varTheta}$	Code	Carrier	
	[mm]	phase	nhaca	[mm]	nhace	nhase	
	BADG	526.4 ± 9.5	Code phase VC: 300 – 700 mm				
	FORT	234.1 ± 10	•			1 4	
	HRAO	666.6 ± 12	(relates to local multi-path				
GPS -	HOB2	2470 + 46	environment)			.3	
	KAII			•	_	3	
	KOKB	709.8 ± 17. •	 Carrier phase VC: 2-5 mm 				
	MATE	376.3 ± 20.	2.0 ± 0.5		JUJ.J ± J.J	3.7 <u>-</u> 0.3	
	NYAL	414.3 ± 10.6	2.1 ± 0.2				



	<i>⊖</i> [mm]	Code phase	Carrier	Θ [mm]	Code nhase	Carrier	
GPS -	BADG	526.4 ± 9.5	Codo pha	do phase VC, 200 700 mm			
	FORT	294.1 ± 10	 Code phase VC: 300 – 700 mm 				
	HRAO	666.6 ± 12	(relates to local multi-path			.4	
	HOB2	317.8 + 16	environm			.3	
	KAII			•	_	.3	
	KOKB	709.8 ± 17. •	Carrier ph	iase VC: 2	2-5 mm	.5	
	MATE	376.3 ± 20.	2.0 ± 0.5	2LUN	JUJ.J <u>+</u> J.J	3.7 _ 0 .3	
	NYAL	414.3 ± 10.6	2.1 ± 0.2				

VLBI

$$\Theta = 2.33 \pm 0.24$$
 []



	<i>⊖</i> [mm]	Code phase	Carrier	(mm)	Code nhase	Carrier		
	BADG	526.4 ± 9.5	Cada aba	Cada abasa V.C. 200 700 mm				
GPS =	FORT	294.1 ± 10	 Code phase VC: 300 – 700 mm 					
	HRAO	666.6 ± 12	(relates to local multi-path					
	HOB2	317.8 + 16	environm		•	.3		
	KAII			•	_	.3		
	KOKB	709.8 ± 17	Carrier ph	nase VC: 2	2-5 mm	.5		
	MATE	376.3 ± 20.	2.0 ± 0.5	2LUN	303.3 <u>-</u> 3.3	5.7 <u>·</u> 0 .3		
	NYAL	414.3 ± 10.6	2.1 ± 0.2					

VLBI

$$\Theta = 2.33 \pm 0.24$$
 []

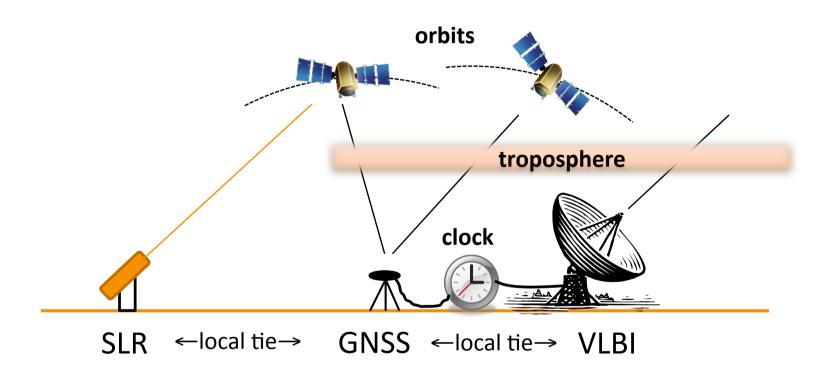
LOCAL TIES
$$\Theta = 12.1 \pm 3.8 \text{ [mm]}$$

Conclusions

- Combination on the observation level works
- Amount of observations highly unbalanced
 - $-N_{GPS} > N_{VLBI} > N_{LOCALTIE}$
- VCE helps to find "natural weights"
 - Shows that formal errors of local ties are too optimistic (note: this does not mean that local ties are not measured that accurate, but rather reflects the fact that other biases do not allow to access the reference points with that accuracy)



The next steps ...



... but first we need to find a way to handle the large number of observations efficiently.



Thank you very much for your attention!



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