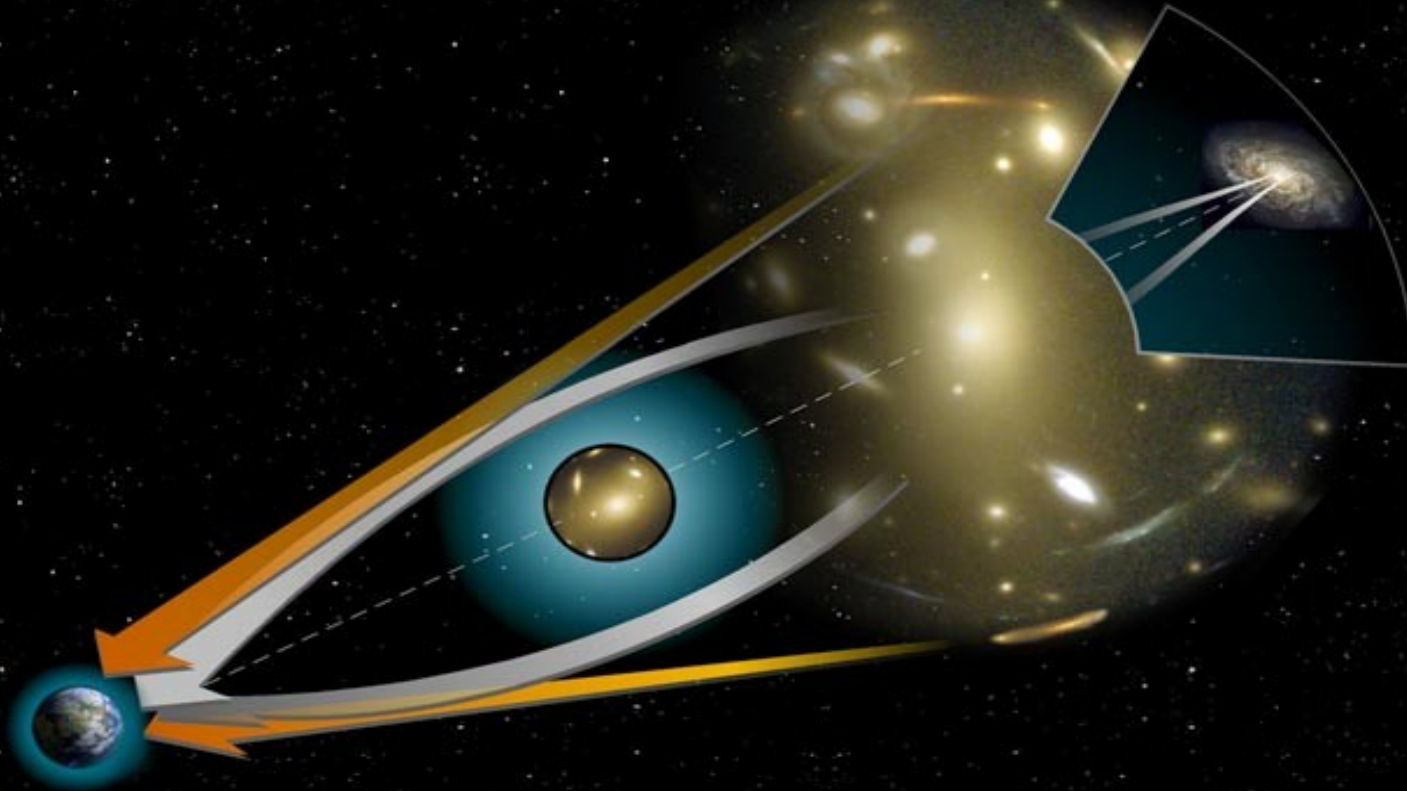


# GRAVITATIONAL LENS

## TIME DELAY MEASUREMENTS WITH AN EFFICIENT METHOD



**GULAY GURKAN**

***SUPERVISOR: NEAL JACKSON***

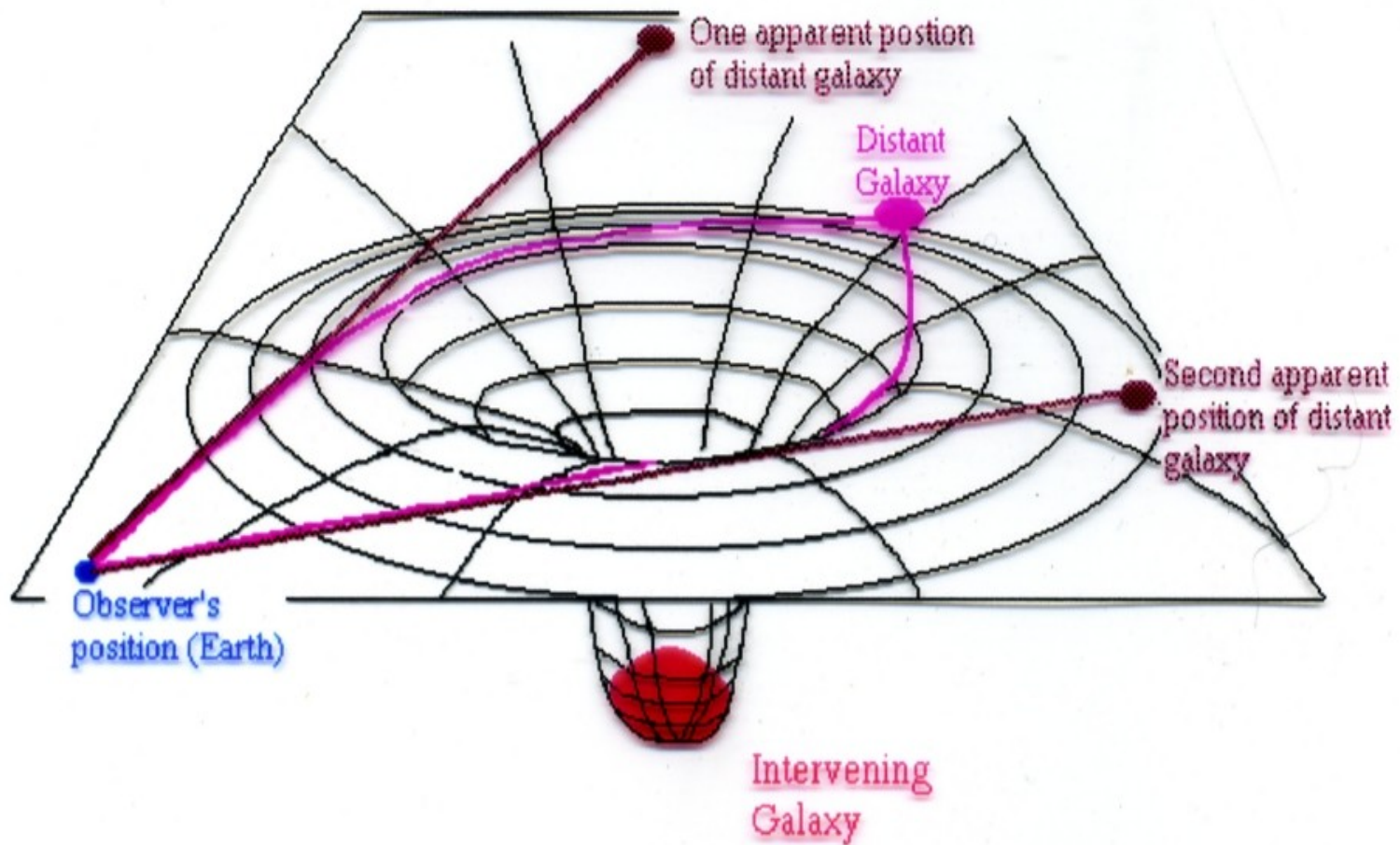
**JODRELL BANK CENTRE FOR ASTROPHYSICS**

**THE UNIVERSITY OF MANCHESTER**

**06.07.2010**

**XL YERAC, Alcala de Henares, SPAIN**

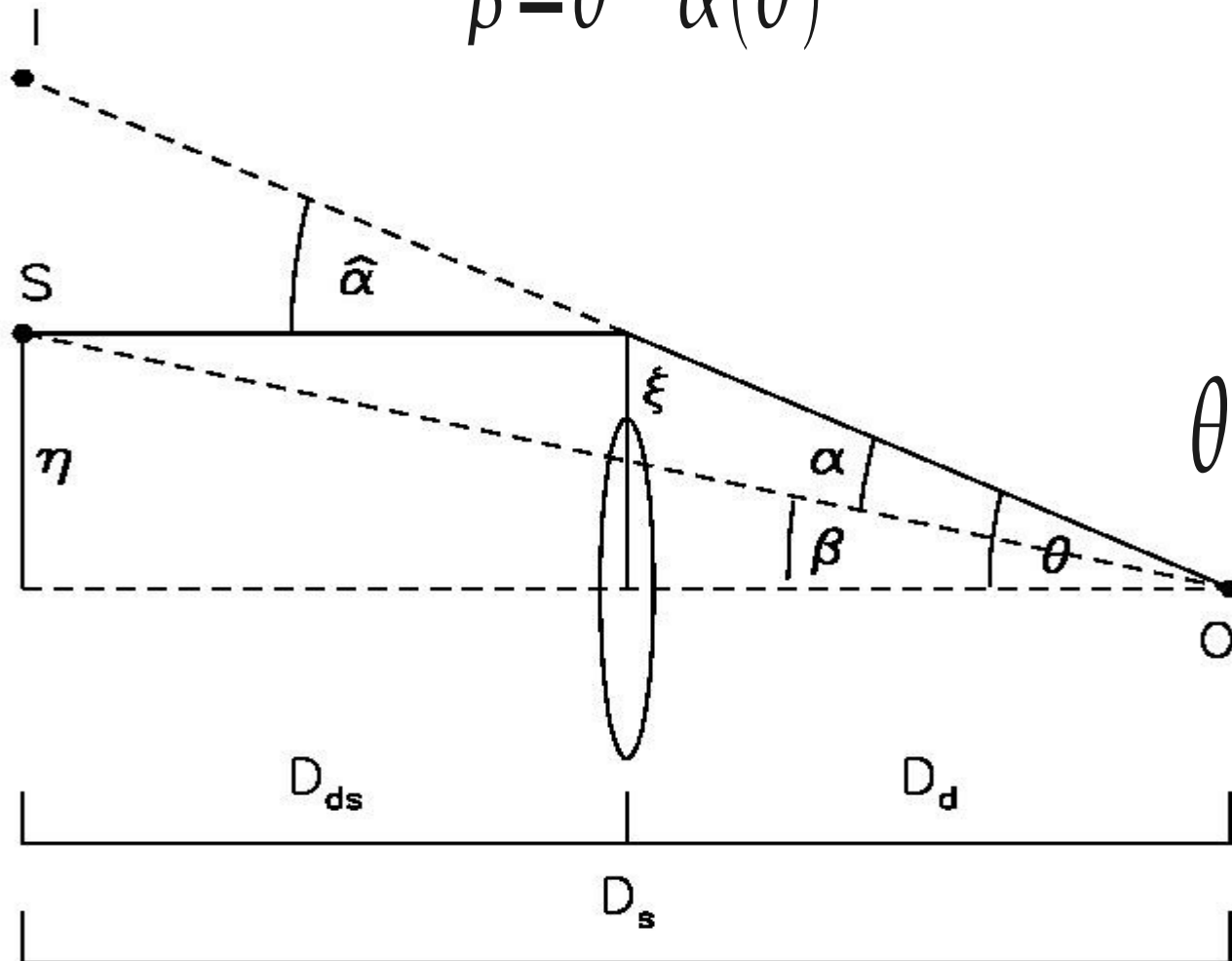
# Gravitational Lensing



# Gravitational Lensing Geometry

## *The Lens Equation*

$$\vec{\beta} = \vec{\theta} - \vec{\alpha}(\vec{\theta})$$



## *The Einstein Radius*

$$\theta_E = \frac{4GM(\theta_E)}{c^2} \frac{D_{ds}}{D_d D_s}$$

# Time Delays

The deflection angle is the gradient of the effective potential;

$$(\vec{\theta} - \vec{\beta}) - \vec{\nabla}_{\theta} \Psi = 0$$

As a gradient;

$$\vec{\nabla}_{\theta} \left[ \frac{1}{2} (\vec{\theta} - \vec{\beta})^2 - \Psi \right] = 0$$

# Time Delays and the Hubble constant

*Total Time Delay = Geometric Delay + Gravitational Delay*

$$\tau(\vec{\theta}) = t_0 \left[ 1/2 (\vec{\theta} - \vec{\beta})^2 - \psi(\vec{\theta}) \right] \quad t_0 = \frac{1 + z_l}{c} \frac{D_l D_s}{D_{ls}}$$

Angular diameter distances for a flat universe;

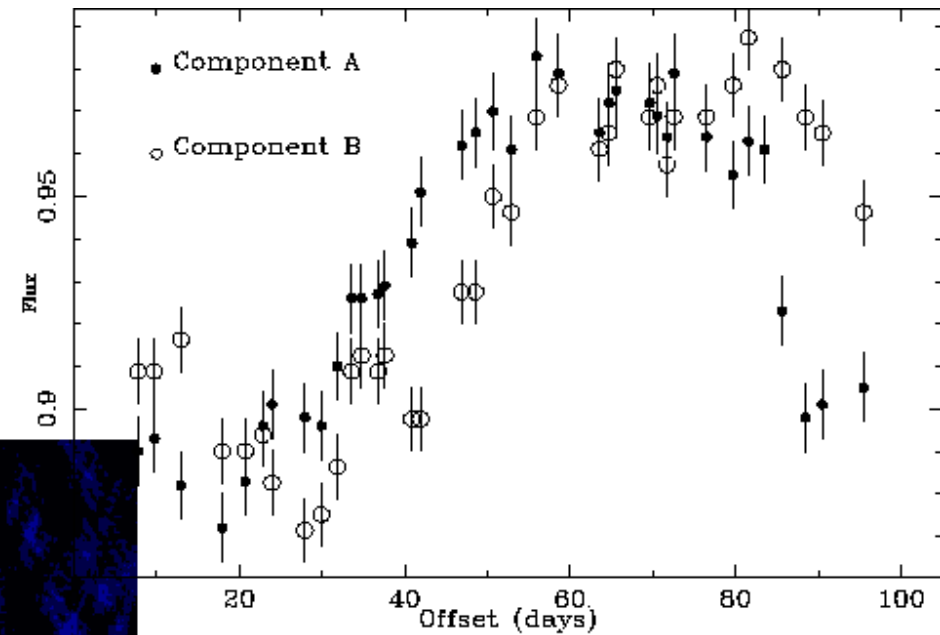
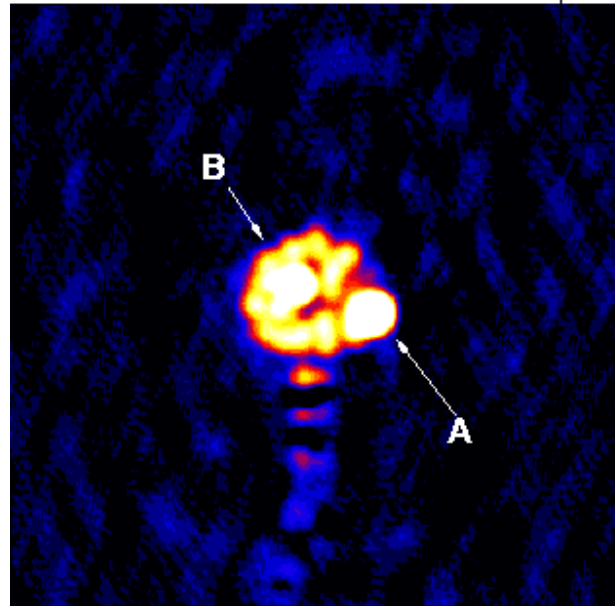
$$D(z_1, z_2) = \frac{c}{H_0} \frac{1}{1 + z_2} \int_{z_1}^{z_2} \frac{dz}{[\Omega_M (1+z)^3 + \Omega_\Lambda]^{1/2}}$$

## The gravitational lens JVAS0218+357

There are about 20  
time delay  
measurements.

IT IS NOT TOO  
MUCH.

Radio map

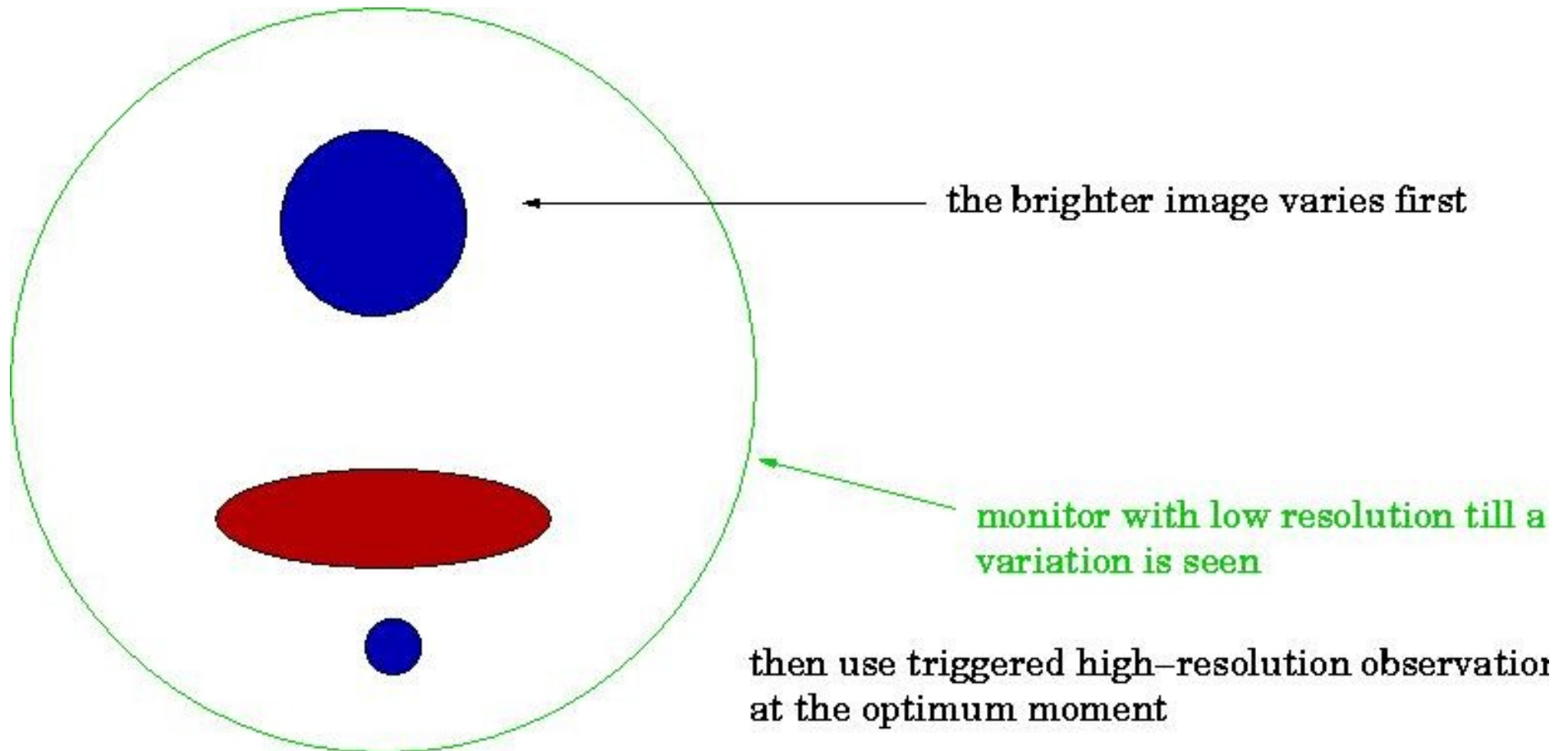


Radio light curves

Time delay =  $10.5 \pm 0.4$  days  
Hubble constant estimate:  
 $69 \text{ km/s/Mpc } (+13/-19, 95\%)$

As long as we know the Hubble constant, we can have a mass model for a lens galaxy or vice versa.

# A New Method to Time Delays



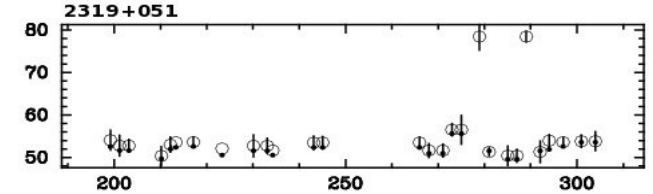
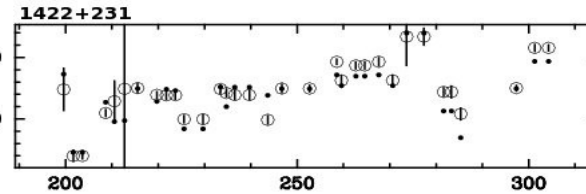
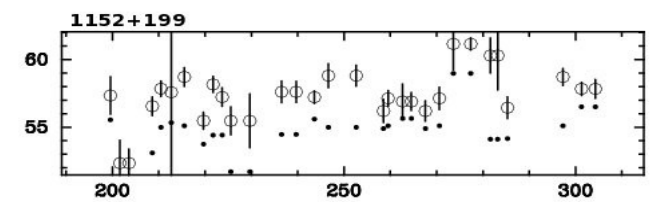
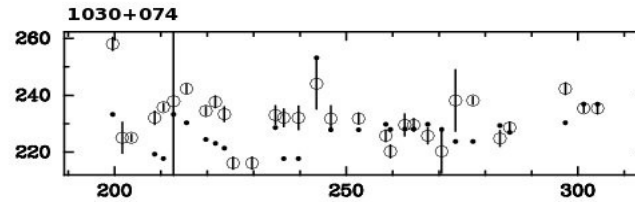
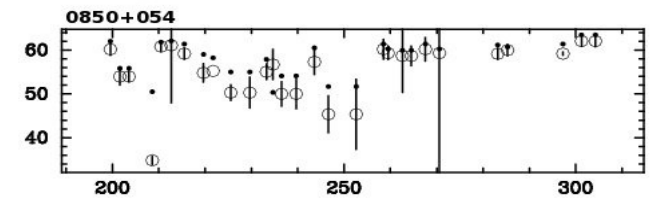
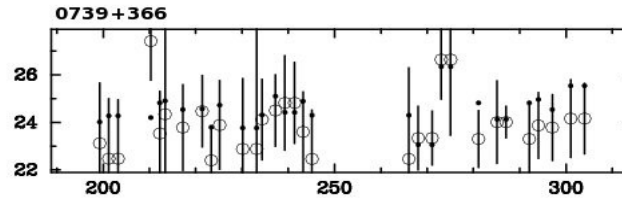
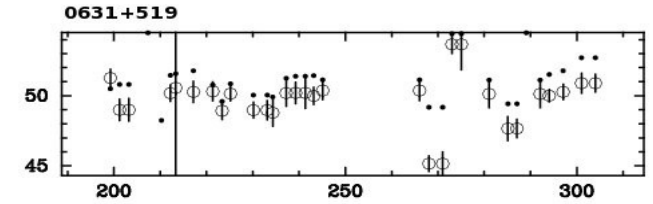
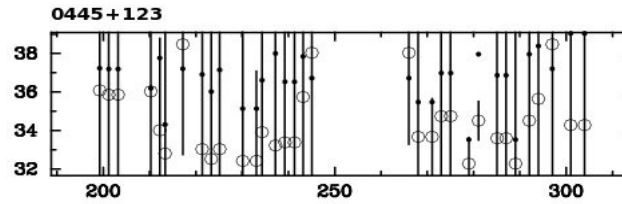
# The WSRT Light Curves

Frequency: 5 GHz

Bandwidth: 160 MHz

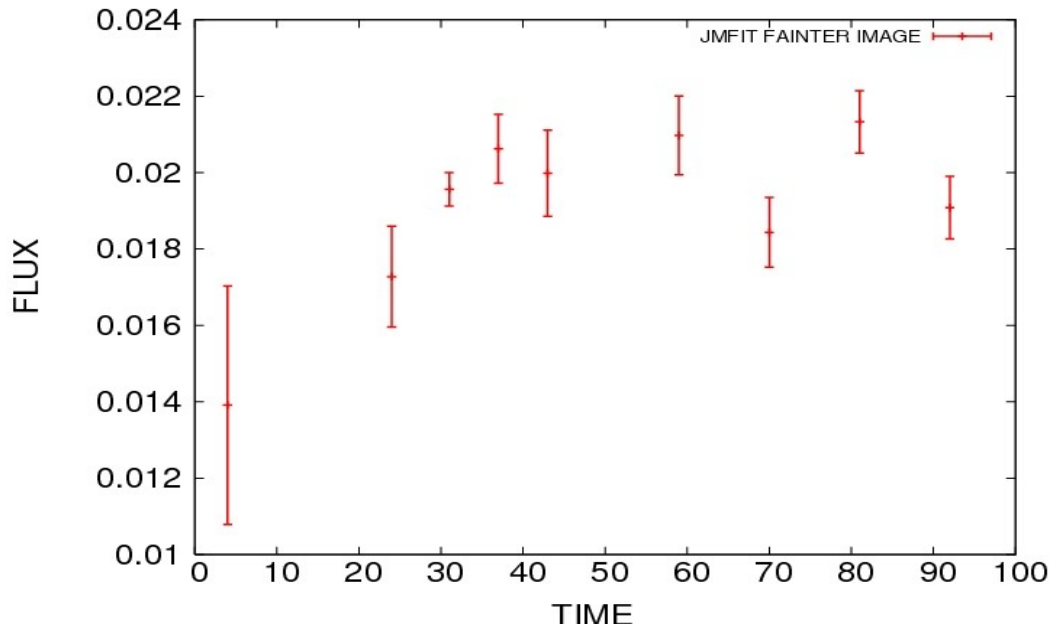
Resolution: 3.7 arcsec

39 epochs





# The VLA Light Curves of B1030+074

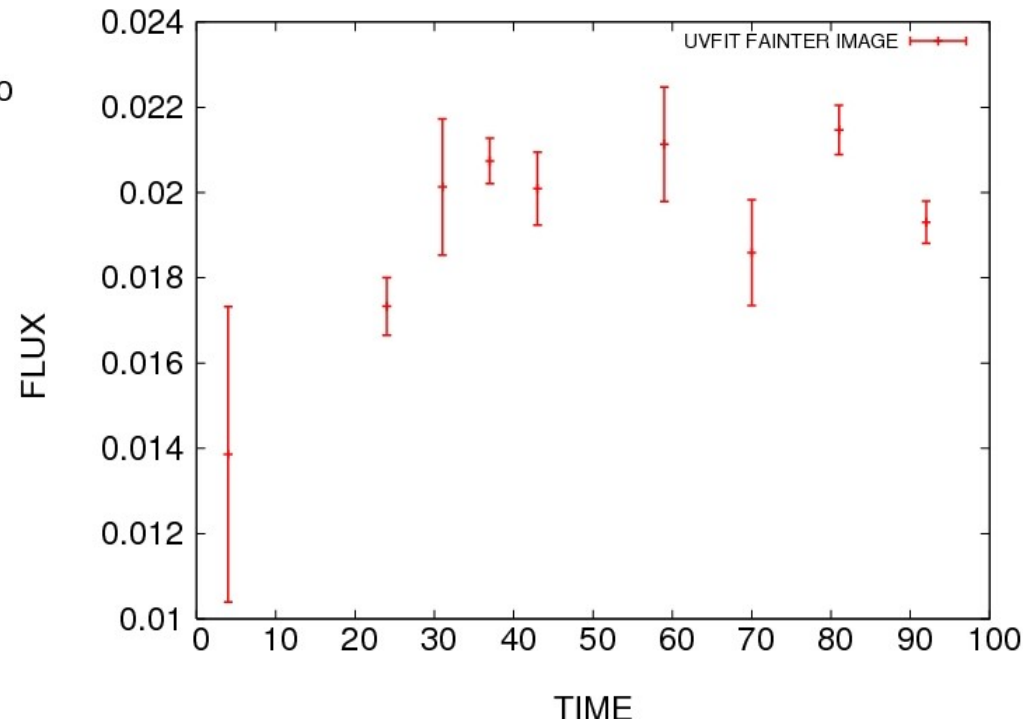


Frequency: 5 GHz

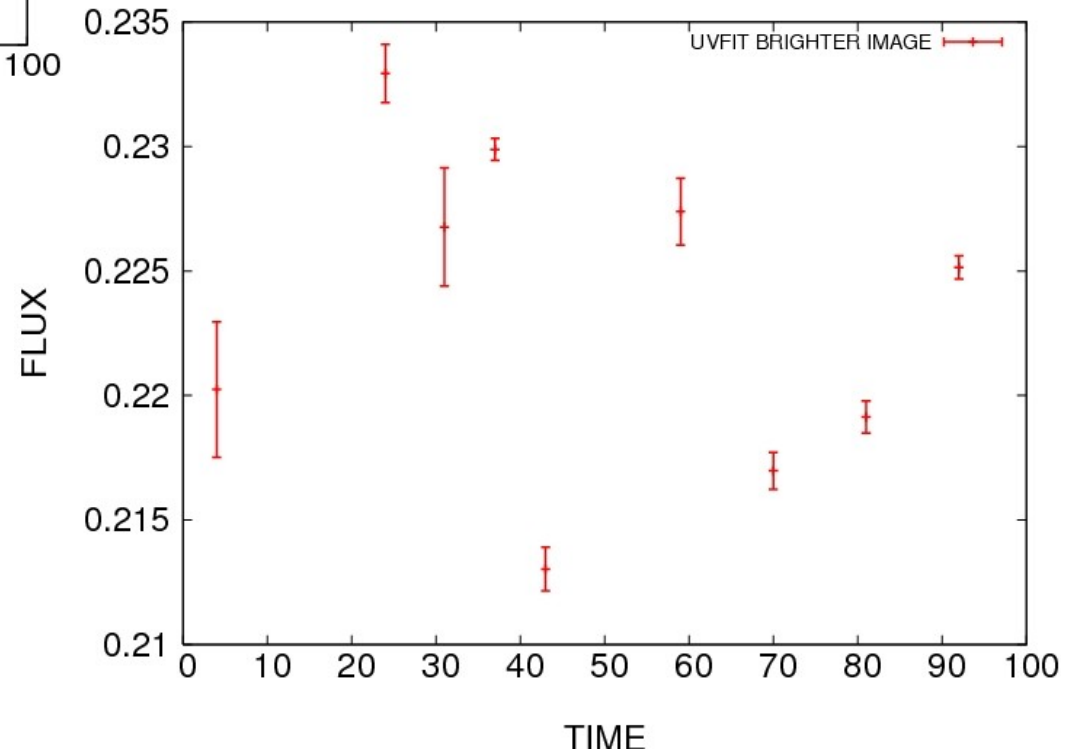
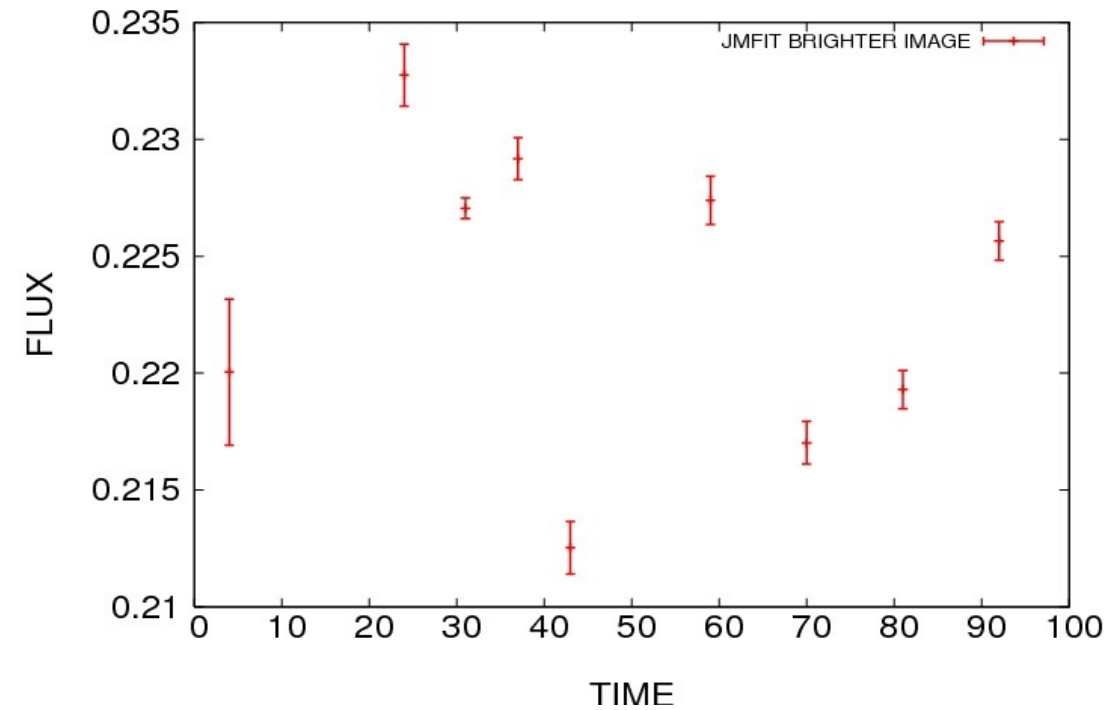
Bandwidth: 100 MHz

Resolution: 0.4 arcsec

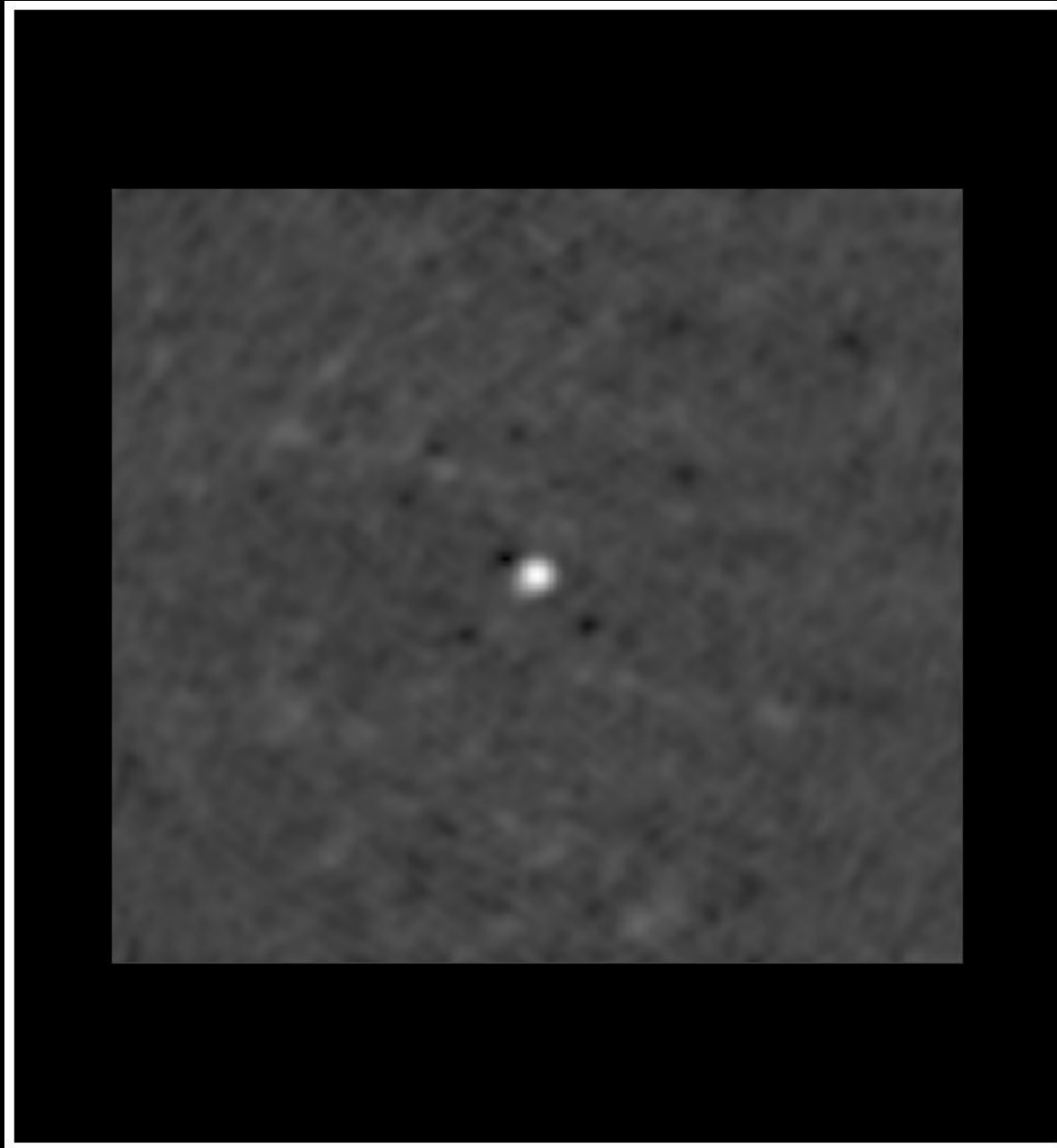
9 epochs



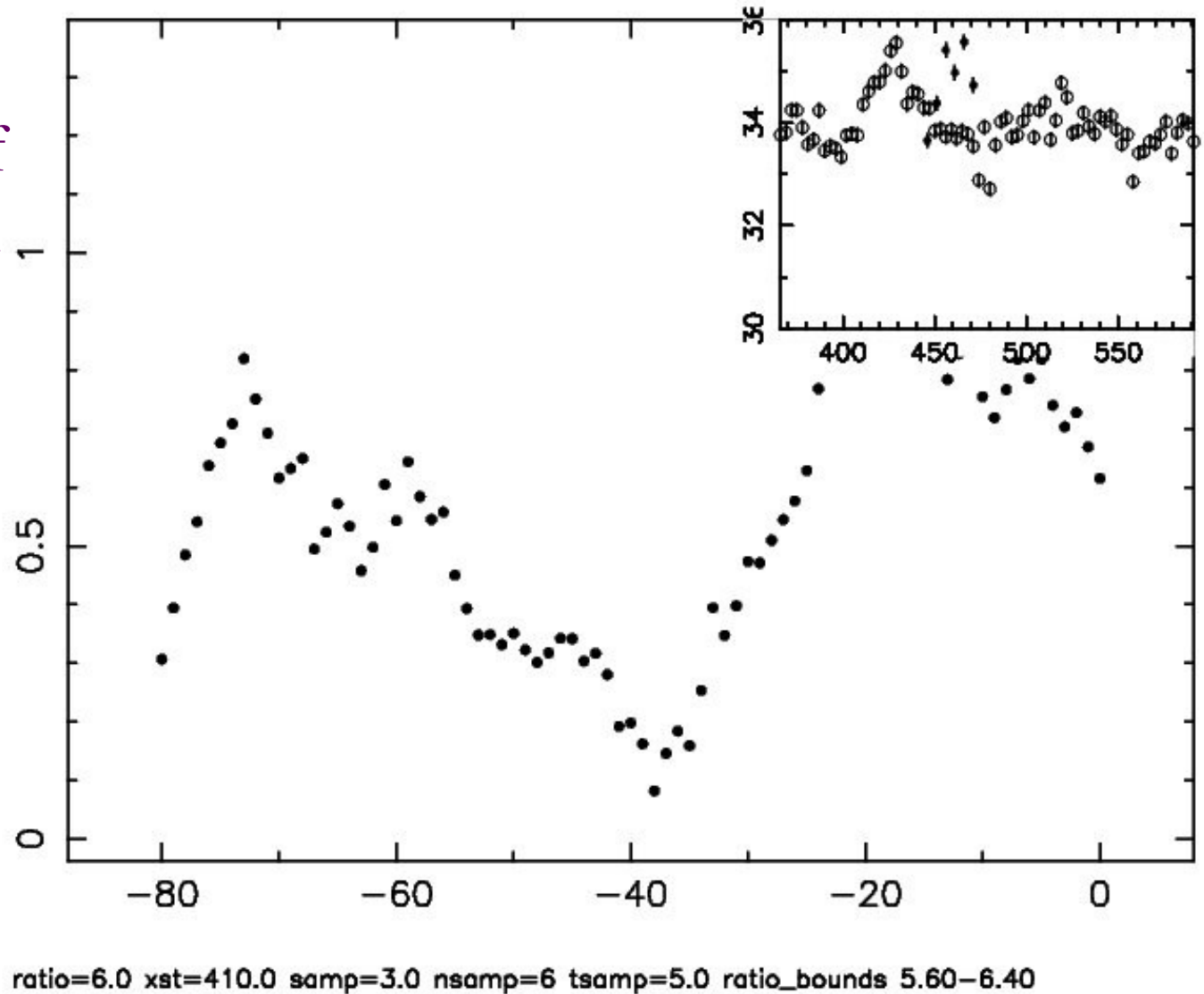
# The VLA Light Curves



# B 1030+074 - Residual Map



Preliminary results of  
Pelt cross-correlation  
simulation...



The clear minimum indicates that a significant cross-correlation is recovered at 38 days and the input value is 36 days.

# Conclusion

Preliminary results show that our new method is sufficient.

**MOREOVER,**

this method is useful since the SKA pathfinders; MeerKAT & ASKAP can be used for time delay measurements.

# Acknowledgement

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